Design Procedure for Interdigital Waveguide Bandpass Filters based on Flat Metallic Strips

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Key Points:

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- A new topology for interdigital bandpass filters based on flat metallic strips is proposed
- A systematic procedure based on the segmentation of the component is presented for the efficient design of the proposed interdigital bandpass filters
- A power handling capability study of the designed interdigital filters is performed

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14 Abstract

In this work, we describe a new topology for interdigital bandpass filters implemented 15 in waveguide technology. Compared to classical coaxial resonators, which are typically 16 based on cylindrical metallic posts, the resonators that we propose are based on rect-17 angular boxed cavities loaded with flat metallic strips of a finite thickness. The main ad-18 vantages of the proposed topology are low-cost practical realization and manufacture sim-19 plicity. The design process, which is based on the classical circuit-based approach com-20 bined with an efficient segmentation of the component, uses the well-known Aggressive 21 Space Mapping technique, with the aim of reducing the overall computation effort. In 22 order to validate the new topology and the design procedure, interdigital bandpass fil-23 ters of orders 3 and 5 operating at the S-band have been designed. For validation pur-24 poses, the results obtained are successfully compared to simulations provided by two dif-25 ferent full-wave electromagnetic tools (i.e., Ansys HFSS and CST Studio Suite). Further-26 more, a multipactor study has also been performed, with the aim of exploring the power 27 handling capability of the proposed filters in view of possible space applications. Finally, 28 the design of classical interdigital filters based on cylindrical posts is also discussed, with 29 the aim of comparing both topologies regarding compactness, as well as in terms of their 30 electrical and high-power performance. 31

32 1 Introduction

33 Bandpass filters based on coaxial resonators, such as filters in combline or interdigital configuration implemented in waveguide technology, are commonly used in mul-34 tiple applications, including space and wireless communications systems (Wang & Yu, 35 2009), (García et al., 2018), (Macchiarella et al., 2018), (Bastioli et al., 2018), (Vallerotonda 36 et al., 2019), (Tamiazzo, 2021), (Zeng et al., 2022), (Yan et al., 2024). Classically, res-37 onators based on rectangular cavities loaded with metallic posts of cylindrical (J. Li et 38 al., 2018), (Boni et al., 2023) or rectangular/square geometry (Arndt & Brandt, 2002), 39 (Kong et al., 2023) have been used in this type of coaxial resonator filters. Other more 40 complex topologies have also been investigated in the past, as the interdigital bandpass 41 filter designed in (Venter et al., 2020), where resonator posts with a triangular cross-section 42 were proposed. Generally, coaxial resonators are coupled by using irises of rectangular 43 geometry, whose position in the structure determines the type of coupling (electric or 44 magnetic) (Jamshidi-Zarmehri et al., 2023), (Zeng et al., 2023). On the other hand, inter-45 resonator coupling can also be controlled by designing the separation between the posts, 46 without the need to insert irises in the component (Z. Li et al., 2023), (Macchiarella et 47 al., 2023). 48

Regarding the state-of-the-art of interdigital bandpass filters based on cylindrical 49 posts, an in-line topology was presented in (Ikram & Rana, 2006), where a fifth-order 50 Chebyshev interdigital bandpass filter operating at C-band was designed. Moreover, a 51 manifold cavity diplexer operating at L-band was designed in (Packiaraj et al., 2005), 52 while a low-loss triplexer that used a combination of a microstrip star junction and three 53 interdigital bandpass filters was proposed in (Munina & Turalchuk, 2015). More recently, 54 a Ku-band 8th-order interdigital filter with an in-line configuration was presented in (J. Li 55 et al., 2018). 56

On the other hand, resonators based on rectangular or square posts have also been 57 widely used in interdigital waveguide filters. For instance, an interdigital cavity filter op-58 erating at Ku-band is designed in (Wu et al., 2019), where two transmission zeros are 59 realized in the frequency response by considering additional resonators outside of the ports 60 of the filter. A further example of an interdigital filter using posts with a rectangular ge-61 ometry can be found in (Jiang et al., 2019), where an eighth-order filter with an improved 62 stop-band suppression is designed. Moreover, a wideband waveguide diplexer based on 63 interdigital filters for mobile base stations is proposed in (Kobrin et al., 2019). Another 64

interesting contribution was presented in (Anand, 2021), where a folded configuration 65 for interdigital filters was proposed in order to implement cross-couplings between the 66 resonators. Additive manufacturing techniques have also been used for designing inter-67 digital filters for radar applications (Rodriguez-Morales et al., 2021), and satellite com-68 munication systems (Venter et al., 2020). More recently, a miniaturized interdigital cav-69 ity filter using loading capacitors is investigated in (Kong et al., 2023). In general, the 70 design process for the bandpass filters presented in the contributions discussed above, 71 is based on the classical approach proposed in (Cameron et al., 2018), so, regardless of 72 the filter order, all the relevant dimensions of the component are optimized at the same 73 time, thus requiring a great computational effort to complete the design process. 74

In this work, a new topology of waveguide bandpass filters based on coaxial res-75 onators implemented in an interdigital configuration is presented. The main novelty of 76 the proposed in-line filter consists in the use of cavities loaded with planar metallic strips 77 of a finite thickness, as shown in Fig. 1, where a third-order interdigital bandpass filter 78 is depicted. A major advantage of this new topology lies in the fact that the filters could 79 be manufactured using low-cost and more simple realization techniques. For instance, 80 the whole structure can be implemented through the cascaded connection of simpler rect-81 angular waveguide sections (including the flat strips), each one manufactured with a CNC 82 (computer numerical control) milling technique. The design procedure that we propose 83 combines the use of the classical circuit-based approach (Cameron et al., 2018) with a 84 strategy based on a segmentation of the structure (San-Blas et al., 2021), (Jamshidi-Zarmehri 85 et al., 2023). 86

In the suggested design procedure, input and output resonators are first designed 87 to achieve the desired external quality factor. After that, the coupling between adjacent 88 resonators is addressed, with the aim of achieving a set of initial values for the physi-89 cal dimensions of the structure. To continue, and specially for high-order filters, a sys-90 tematic design procedure based on the segmentation of the whole component is proposed. 91 In this procedure, the different resonators of the filter are added one after the other, thus 92 dividing the design process in more simple steps, while also reducing the number of vari-93 ables to be optimized in each stage. Equivalent circuit models are also important in this 94 approach, since their electrical responses will be used as target curves in all optimiza-95 tion stages of the design procedure. Furthermore, the Aggressive Space Mapping (ASM) 96 technique (Bandler et al., 1995) has also been used in this work, so that most of the op-97 timizations performed during the design process are carried out very efficiently in a low-98 precision simulation space (the coarse model). 99

In order to validate the new topology that we propose, two interdigital bandpass 100 filters operating at S-band have been designed. The correct electrical performance of the 101 filters is successfully validated using two different electromagnetic (EM) simulation tools 102 (Ansys HFSS, and CST Studio Suite). In addition, a multipactor study (Berenguer et 103 al., 2019) is also performed for both filters, in order to evaluate the high-power perfor-104 mance of this new topology under high-vacuum conditions. Furthermore, the design of 105 classical interdigital filters based on cylindrical posts is also discussed, with the aim of 106 comparing both topologies in terms of compactness, electrical performance and power 107 handling capability. 108

¹⁰⁹ 2 Design of the coaxial resonator and related equivalent circuit

The basic coaxial resonator proposed in this work is shown in Fig. 2. It is based on a rectangular cavity loaded with a thick metallic strip. The strip is connected to the base of the resonator at one end. At the other end, there is an open circuit or gap, as shown in Fig. 2. In addition, the metal strip is located in the center of the rectangular enclosure. The relevant dimensions of the resonator are designed with the objective of having a resonance at the center frequency f_0 of the filter. In this work, two bandpass



Figure 1. Third-order symmetric interdigital bandpass filter with flat metallic strips.

filters of orders N=3 and N=5 will be designed. Since both of them share the same center frequency ($f_0 = 3$ GHz), the resonator designed in this section will be used in both bandpass filters.

In order to design the resonator, the full-wave EM simulator Ansys HFSS has been 119 used. First of all, an access port located at the y = 0 plane of the structure in Fig. 2, 120 has been opened. It is important to note that, with this access port, the resonator be-121 comes a section of coaxial guide, with internal and external rectangular contours, loaded 122 by a length of short-circuited rectangular waveguide. To continue, the phase of the S_{11} 123 parameter at the input port is calculated, and the dimensions of the resonator are op-124 timized until the phase of S_{11} is equal to 180° at a frequency equal to f_0 . The final di-125 mensions (all expressed in mm) of the optimized resonator are as follows (see Fig. 2): 126 $a_r = b_r = 26$, $l_r = 7$, H = 23.233, w = 5 and t = 1. It is important to note that the di-127 mensions a_r, b_r, l_r (dimensions of the rectangular enclosure), w and t (width and thick-128 ness of the strip) will remain fixed, and will not be optimized during the filter design pro-129 cess. 130

In addition, we are also interested in obtaining an equivalent circuit of the resonator based on lumped elements. This equivalent circuit consists of a series combination of an inductance L and a capacitor C. With the aim of obtaining the equivalent series network, the slope parameter X of the optimized coaxial resonator is first calculated from the simulated results (Matthaei et al., 1980):

$$X = \frac{w_0}{2} \left. \frac{dX_{in}(w)}{dw} \right|_{w=w_0} = 295.48\,\Omega \tag{1}$$

where $w_0 = 2\pi f_0$, and X_{in} represents the reactance of the input impedance of the optimized resonator. Then, the value of the equivalent inductance of the resonator can be calculated as: $L = X/w_0 = 15.676$ nH. The value of the equivalent capacitance can now be computed using: $C = 1/(w_0^2 L) = 0.179$ pF.

The unloaded Q factor of the designed resonator has been calculated using Ansys 140 HFSS. In this analysis, an equivalent conductivity value of $38 \cdot 10^6$ S/m (aluminium) 141 has been considered, thus obtaining $Q_u = 1462$. Furthermore, we have computed both 142 the unloaded Q factor and the resonant frequency (f_0) of the designed resonator in terms 143 of the height H of the strip, and also as a function of the length l_r of the rectangular en-144 closure. The obtained results are shown in Fig. 3. As we expected, when the height of 145 the strip decreases (thus increasing the gap between the strip and the top wall of the en-146 closure), both Q_u and f_0 increase (see Fig. 3, left). As it is well known, the cited gap 147 represents a critical region in terms of high-power performance in classical coaxial res-148 onator filters. Nevertheless, since the thickness of the strip used in our proposed resonator 149



Figure 2. Coaxial resonator loaded with a flat metallic strip.



Figure 3. Variation of the unloaded Q factor and the resonant frequency of the flat strip resonator in terms of H and l_r .

is small (only 1 mm), the equivalent capacitance in this region is less significant than the
 one found in classical resonators based on cylindrical posts. Therefore, an increased high power performance is expected compared to classical interdigital filters, as it is discussed
 in Section 6.

On the other hand, as it can be observed in Fig. 3 (right), when the length of the 154 rectangular enclosure decreases (thus obtaining a more compact resonator), Q_u decreases 155 (thus increasing the losses, as well), while f_0 increases. Furthermore, for comparison pur-156 poses, we have also analysed the unloaded Q factor of a classical resonator loaded with 157 a cylindrical post. In this design, the post diameter has been chosen to be equal to the 158 width w of the flat strip, while the dimensions of the rectangular enclosure are the same 159 that we have used in the flat strip resonator. The computed Q factor is $Q_u = 937$, so 160 the novel resonator proposed in our work has a better performance in terms of losses than 161 the classical solution based on cylindrical posts. 162



Figure 4. Equivalent circuit network of the 3rd-order interdigital bandpass filter.



Figure 5. Frequency response of the equivalent circuit network shown in Fig. 4.

¹⁶³ 3 Equivalent circuit of the bandpass filters

The purpose of this section is to obtain an equivalent network to characterize the 164 designed bandpass filters. The electrical response of this equivalent circuit will be used 165 to generate target curves to obtain the in-band response of the designed filter using it-166 erative optimizations. The equivalent circuit of the filters will be composed of the cas-167 cade connection of ideal impedance inverters (which will characterize both the input/output 168 couplings and also the inter-resonator couplings) and series L-C networks (which will model 169 the resonators). It is also worth noting that, as it is well known, transmission zeros can-170 not be realized using coaxial resonators in a standard in-line interdigital configuration. 171

The electrical specifications for the 3rd-order interdigital filter that will be designed in Section 4 are: center frequency $f_0 = 3$ GHz, return loss of RL = 25 dB, and bandwidth BW = 200 MHz. Given these specifications, the values (in Ω) of the impedance inverters, which have been calculated using the slope parameter X of the resonator, are as follows: $K_{01} = K_{34} = 86.394$ and $K_{12} = K_{23} = 24.027$ (Matthaei et al., 1980). The equivalent circuit of the 3rd-order filter is shown in Fig. 4, while its frequency response is displayed in Fig. 5.

¹⁷⁹ 4 Design of a 3rd-order bandpass filter following a classical approach

In this section, the procedure used to design a third-order Chebyshev bandpass filter (electrical specifications: $f_0 = 3$ GHz, RL = 25 dB, BW = 200 MHz) is described in detail. As we have previously mentioned, in this case, where the order of the filter is not high, the design process is based on the classical approach proposed in (Cameron et al., 2018). First, input and output couplings are characterized and, after that, the interresonator couplings are calculated. Finally, the complete filter is assembled and all di-



Figure 6. External quality factor in terms of the distance d.

mensions are optimized using as a target the response of the corresponding equivalent
 circuit (see Fig. 5).

First, the design of the excitation of the input and output resonators is discussed. 188 These resonators are fed with SMA coaxial waveguides ($\epsilon_r = 2.2$), with external and in-189 ternal radii of 2.05 and 0.65 mm, respectively. The metallic strips of the input/output 190 resonators are in contact with a metal feeding probe, located at a distance d from the 191 bottom of the cavity, as shown in Fig. 1. The distance d will be optimized in order to 192 obtain the required external quality factor Q_{ext} . This parameter can be obtained follow-193 ing the method detailed in (Cameron et al., 2018), namely, by evaluating the group delay of parameter S_{11} at frequency f_0 . Fig. 6 shows the dependence of the external qual-195 ity factor in terms of the distance d. On the other hand, the required value for Q_{ext} can 196 be calculated as follows (Cameron et al., 2018): 197

$$Q_{ext} = \frac{f_0}{BWm_{01}^2} = 10.055 \tag{2}$$

where $m_{01} = 1/\sqrt{g_0g_1}$ (being g_0 and g_1 the corresponding low-pass prototype elements). Furthermore, Q_{ext} is related to K_{01} through $Q_{ext} = (XZ_0)/K_{01}^2$, where $Z_0 = \eta_0/\sqrt{\epsilon_r} = 253.9 \ \Omega$ represents the modal impedance of the TEM mode of the coaxial waveguide port. In view of the value obtained for the required external quality factor, an initial value $d = 7.321 \ \text{mm}$ can be deduced from Fig. 6.

Once the couplings of the input/output resonators have been obtained, the cou-203 plings between adjacent resonators are characterized as a function of the spacing s be-204 tween the strips (see Fig. 1). For this purpose, a symmetrical two-port component is con-205 sidered, consisting of two resonators weakly coupled to the input and output coaxial ports. 206 It is well known that the resonant frequencies of this component are related to the value 207 of the electromagnetic coupling k of the structure, which can be obtained as a function 208 of the separation s between strips, as shown in Fig. 7. Since the required value for the 209 electromagnetic coupling between resonators #1 and #2 can be computed as $k_{12} = K_{12}/(w_0 L) =$ 210 0.0813, an initial value of s = 14.774 mm can be deduced from Fig. 7. 211

At this point, it would be interesting to determine the nature of the coupling (electric or magnetic) between two interdigital resonators based on flat metallic strips. First,



Figure 7. Electromagnetic coupling between adjacent resonators as a function of the separation *s* between strips.



Figure 8. Magnitude and phase of the S_{21} parameter when the resonators are in (a) a combline configuration and in (b) an interdigital configuration.

let us consider two resonators coupled in a combline configuration, both weakly coupled 214 to the coaxial input/output ports (the dimensions of the strips and the dimensions of 215 the resonator have been deduced in Section 2). In this component, note that both res-216 onator strips are connected to the bottom of the filter. In addition, a separation of s =217 14 mm between the resonators has been used for this simulation. It is well-known that, 218 in this type of structure, the nature of the predominant coupling is magnetic (Thomas, 219 2003). Moreover, Fig. 8(a), which can be used to determine the magnitude of the elec-220 tromagnetic coupling k (Cameron et al., 2018), shows the magnitude and the phase of 221 the S_{21} parameter of the considered combline structure. On the other hand, Fig. 8(b) 222 shows this same information when the two resonators are in an interdigital configura-223 tion. As we can observe, there is a phase shift of 180° between the S_{21} phase responses 224 of the two cases analyzed, thus confirming a change in the sign of the predominant cou-225 pling. In this regard, it is important to note that the combline-type coupling (of mag-226 netic nature) is approximately one order of magnitude lower than the interdigital one 227 for the same resonator separation, thus making the non-adjacent couplings negligible in 228 the interdigital case and, thereby, facilitating the proposed systematic in-line design. 229



Figure 9. S-parameters of the designed 3rd-order interdigital filter. Comparison of results obtained with Ansys HFSS and CST Studio Suite.

In the next step of the design process, the complete filter is assembled (consider-230 ing symmetry in the component) and the filter dimensions H_1, H_2, s and d (see Fig. 1) 231 are optimized in a low-accuracy space, until recovering the target response. The values 232 obtained are (all in mm) $H_1 = 23.380$, $H_2 = 20.144$, s = 18.606 and d = 5.491. All sim-233 ulations previously described have been performed using the full-wave EM tool FEST3D 234 (which is part of CST Studio Suite), with a set of parameters chosen to obtain very fast 235 low-accuracy results. For instance, only 10 accessible modes (Conciauro et al., 2000) were 236 considered in all simulations concerning the design process of this filter. Consequently, 237 the resulting low-accuracy frequency response is not sufficiently precise for fabrication 238 purposes. However, the well-known ASM technique presented in (Bandler et al., 1995) 239 allows us to refine these results by transforming the low-accuracy data (coarse model) 240 into a high-precision solution (fine model). In this design, FEST3D serves as the coarse 241 model, while the finite-element EM tool Ansys HFSS is used as the fine model. In most 242 cases, only a few iterations are required to obtain the target frequency response of the 243 filter in the fine space. 244

The final dimensions obtained with the ASM procedure (in mm) are as follows: $H_1 =$ 245 23.683, $H_2 = 20.320$, s = 17.721 and d = 6.076. In order to further validate both the 246 topology of the new filter and the design procedure we have followed, the filter has been 247 analyzed using an additional EM simulator, namely, CST Studio Suite. The results ob-248 tained are shown in Fig. 9, where an excellent agreement between the results provided 249 by HFSS and CST can, indeed, be observed. We have also included in the same figure 250 the S-parameters of the filter designed in the low-precision space to show that a very good 251 agreement between the results obtained in both simulation spaces (low and high-precision 252 models) has been achieved. Furthermore, the response in the fine space with the opti-253 mum dimensions found in the coarse space has also been included in Fig. 9 for compar-254 ison purposes (see label "Initial point"). 255

At this point, it is important to discuss the design of classical interdigital filters based on cylindrical posts, with the aim of comparing this classical topology to the novel proposed flat strip configuration, both in terms of compactness and electrical performance. In this context, we have first designed a resonator ($f_0 = 3$ GHz) loaded with a cylindrical post whose diameter is equal to the width w of the flat strip that we have used in our previous design (the dimensions of the rectangular enclosure used in this resonator can be found in Section 2). Afterwards, the inter-resonator couplings have been com-



Figure 10. Electrical responses of the designed 3rd-order interdigital bandpass filters based on cylindrical posts and flat strips.

puted to determine the initial values for the different separations between resonators. Our results show that such initial values are very similar to the ones obtained when resonators based on flat strips are considered. We can, therefore, estimate that the final filter lengths for both considered topologies are comparable, so the compactness of our novel filter topology based on flat strips resonators is very similar to the one obtained with classical resonators loaded with cylindrical posts.

To validate this statement, a 3rd-order interdigital bandpass filter including res-269 onators based on cylindrical posts has been designed following the approach previously 270 detailed. The only difference is that, in this case, after computing the initial values for 271 all relevant filter dimensions, a brute-force optimization algorithm has been used (instead 272 of the ASM technique) in order to obtain the filter dimensions in a high-precision space. 273 In this design, we have used the same coaxial excitation and the same electrical spec-274 ifications that we employed for the 3rd-order filter based on flat strips. The dimensions 275 of this filter (all in mm) are: $H_1 = 22.70$, $H_2 = 19.56$, s = 18.54 and d = 5.40, where s 276 represents the separation between the centres of the cylindrical posts (see also Fig. 1 for 277 the definition of these variables by considering cylindrical posts). The total length of the 278 designed filter (high-precision space) is 44.1 mm, while the length of the 3rd-order fil-279 ter based on flat strips previously designed is equal to 44.4 mm, thus confirming that both 280 topologies exhibit an almost identical performance in terms of compactness. The in-band 281 frequency responses (obtained using Ansys HFSS) of both 3rd-order filter topologies are 282 shown in Fig. 10. 283

Regarding the insertion loss, we have considered a finite conductivity of $38 \cdot 10^6$ 284 S/m (aluminium) in our analysis, and we have obtained that the insertion loss mean value 285 is equal to 0.1 dB in the nominal passband (2.9 - 3.1 GHz) for both topologies. It is im-286 portant to note at this point that, although the two filters have been designed with the 287 same electrical specifications, the bandwidth of the filter based on cylindrical posts gets 288 slightly higher than the bandwidth of the filter based on flat strips (see also Fig. 10). This 289 fact explains why both filters present a very similar insertion loss, even though the res-290 onator based on flat strips exhibits a higher unloaded Q factor. 291

We have also calculated the insertion loss of the 5th-order interdigital filter based on flat strips presented in the next section. In this case, the mean value in the nominal passband is of 0.24 dB. It is worth noting that the obtained values are consistent with



Figure 11. Broadband response of the designed 3rd-order interdigital bandpass filters.

the theoretical insertion loss computed using the analytical formulas found in the technical literature for the prescribed specifications.

On the other hand, and regarding the broadband performance, Fig. 11 shows the out-of-band response of the designed 3rd-order interdigital filter based on cylindrical posts (red lines) compared to the response of the filter based on flat strips (blue lines). It is worth mentioning that the interdigital filter based on flat strips shows an out-of-band rejection starting at higher frequencies, and a wider spurious-free range, when compared to the classical filter based on cylindrical posts. Therefore, the novel topology proposed in this work enhances the out-of-band performance of classical interdigital filters.

As we have mentioned before, a 3rd-order interdigital bandpass filter including res-304 onators based on cylindrical posts has been designed using a brute-force algorithm to 305 obtain the filter dimensions in a high-precision space. In particular, after obtaining an 306 initial set of filter dimensions following the classical design approach, the whole compo-307 nent is assembled. Next, by means of a full-wave simulator (Ansys HFSS), the dimen-308 sions of the physical structure are iteratively optimized until the desired electrical re-309 sponse is recovered. Proceeding in this way, the complete set of the filter dimensions (4 310 dimensions in this case) is optimized at the same time. Compared to the design strat-311 egy based on the ASM technique, the design approach based on a brute-force design al-312 gorithm spends, approximately, 19% more computational time. In addition, it is worth 313 noting that this conclusion stands for a third-order interdigital filter. Therefore, if a high-314 order filter needs to be designed, the number of involved physical dimensions will be higher 315 and the cited increase in CPU time could be even more significant, since the brute-force 316 algorithm does not benefit from the segmentation technique proposed in this work. 317

³¹⁸ 5 Design of a 5th-order bandpass filter using a segmentation technique

In this section, the design of a fifth-order interdigital bandpass filter with a Chebyshev response is addressed. The technique proposed for the efficient design of this highorder filter is based on a segmentation of the component, where the different resonators of the filter are progressively added one after the other, with the aim of reducing the number of variables to be optimized in each step of the design process. The electrical response (i.e., the group delay of the S_{11} parameter) of the equivalent circuit of the structure used in each step, will be used as the target curve in the optimization process. After that, the



Figure 12. Fifth-order interdigital bandpass filter with flat metallic strips.

ASM technique will be used again to obtain the final dimensions. Fig. 12 shows the topology of the 5th-order filter under consideration.

The center frequency chosen for this bandpass filter is the same as the one we used 328 for the 3rd-order filter. Therefore, both the resonator dimensions and the values of the 329 equivalent L-C series network have been already calculated in Section 2. The equivalent 330 circuit of this filter, as explained in Section 3, consists of the cascade connection of L-331 C series networks and ideal impedance inverters. Given the electrical specifications of 332 the 5th-order filter ($f_0 = 3$ GHz, RL = 25 dB, BW = 150 MHz), the following values 333 (in Ω) of the impedance inverters can be readily deduced: $K_{01} = K_{56} = 68.658, K_{12} =$ 334 $K_{45} = 14.387, K_{23} = K_{34} = 10.083.$ 335

5.1 Design of the coaxial excitation

First, the design of the coaxial excitation of the input/output resonators of the bandpass filter is addressed. The dimensions of the coaxial waveguide ($\epsilon_r = 2.2$) are the same ones used in the 3rd-order filter (external and internal radii of 2.05 and 0.65 mm, respectively). In order to characterize the external quality factor Q_{ext} , we follow the same method explained for the 3rd-order filter. In this case, since the required quality factor is $Q_{ext} =$ 15.921, an initial value of d = 5.053 mm can be deduced from Fig. 6.

³⁴³ 5.2 Inter-resonator coupling

The inter-resonator couplings depend on the separation $s_{i,j}$ between the resonator strips (see Fig. 12). The required electromagnetic couplings between resonators can be computed as:

$$k_{1,2} = \frac{K_{1,2}}{w_0 \cdot L} = 0.0487 \tag{3}$$

$$k_{2,3} = \frac{K_{2,3}}{w_0 \cdot L} = 0.0341 \tag{4}$$

Therefore, the following initial values for the separation between resonators can be deduced from Fig. 7: $s_{1,2}=19.236$ mm and $s_{2,3}=22.551$ mm.

³⁴⁹ 5.3 Systematic design using a step-by-step procedure

Once we have obtained a set of initial values for the relevant dimensions, we continue our filter design following a step-by-step strategy. The design process is based on the segmentation of the filter, where the different resonators are added one after the other,



Figure 13. Electrical response of the waveguide structure considered in the first stage compared to the ideal response.

with the aim of reducing the number of variables to be optimized in each stage. The electrical response of the lumped-element equivalent circuit of the structure used in each step will be used as the target response. The optimized dimensions obtained in each step will then be used as initial values in the next step of the design process. This design procedure will be concluded with the ASM technique. All the simulations discussed in the next sections have been performed in a low-precision space using the EM software FEST3D.

359 5.3.1 First stage

In the first step of the design process, the component under consideration consists 360 of the first two resonators of the interdigital filter (see Fig. 12) fed by a coaxial probe. 361 It is worth noting that there is only one access port in this structure. The equivalent cir-362 cuit of this waveguide component consists of the cascade connection of the input trans-363 mission line, inverter $K_{0,1}$, an L-C series network representing the first resonator, impedance 364 inverter $K_{1,2}$, and another L-C series network short-circuited at its end. In this first stage, 365 the dimensions to be optimized are the heights H_1 and H_2 of the strips, the separation 366 $s_{1,2}$ between resonators, and the height d of the feeding probe (see Fig. 12). In this first 367 stage, the set of dimensions obtained in the previous sections are used as a starting point 368 in the optimization process. 369

Next, the dimensions of the waveguide component are optimized using, as a tar-370 get response, the group delay of the S_{11} parameter of the circuit model. The results of 371 the optimization are shown in Fig. 13, where a very good agreement can be observed be-372 tween both set of data. The values obtained (in mm) for each dimension at the end of 373 the optimization process are: $H_1 = 22.942$, $H_2 = 22.205$, $s_{1,2} = 19.059$ and d = 4.522. 374 On the other hand, the set of initial dimensions used as a starting point in this first stage 375 are: $H_1 = H_2 = 23.233$, $s_{1,2} = 19.236$ and d = 5.053 (the response of this initial point 376 has also been included in Fig 13). As we can see, the optimized final values are, indeed, 377 very close to the initial values. 378



Figure 14. Electrical response of the waveguide structure considered in the second stage compared to the ideal response.

379 5.3.2 Second stage

In the second stage of the design process, a new resonator is added to the struc-380 ture, thus obtaining a waveguide structure composed of the first three resonators of the 381 filter (see Fig. 12). The circuit model of this structure can be readily obtained by adding 382 to the circuit network of the previous step, the inverter $K_{2,3}$, and a new L-C series net-383 work. Next, the dimensions of this waveguide structure must be optimized to obtain the 384 same electrical response of the ideal network. The parameters to be optimized in this 385 stage are the same as in the previous step $(H_1, H_2, s_{1,2} \text{ and } d)$, including also the height 386 H_3 of the third resonator, and the separation $s_{2,3}$ between the second and third resonators 387 (see also Fig. 12). The results of this optimization are shown in Fig. 14, where an ex-388 cellent agreement is again observed between the response of the lumped-element model and the full-wave simulation. The final values (in mm) for the optimized dimensions are: 390 $H_1 = 22.955, H_2 = 20.108, H_3 = 21.994, s_{1,2} = 22.226, s_{2,3} = 25.176$ and d = 4.382. The 391 corresponding starting points are the final values obtained at the end of the previous stage. 392 We have also included in Fig. 14 the response of the initial point from where the match-393 ing to the group delay reference curve is performed. 394

5.3.3 Third stage

395

At this point of the procedure, we have completed the design of one half of the band-396 pass filter, since the component is symmetrical. Therefore, the optimization of the whole 397 filter can be performed next by taking into account that (see Fig. 12): $H_1 = H_5$, $H_2 =$ 398 H_4 , $s_{1,2} = s_{4,5}$ and $s_{2,3} = s_{3,4}$. In this final stage of the design process, the S-parameters 399 of the equivalent lumped-element network of the 5th-order filter are used as the target 400 response, and all the dimensions of the structure are optimized. The optimization re-401 sults are shown in Fig. 15, where an excellent agreement is observed between the full-402 wave EM-simulation, and the response of the ideal network, thereby validating the sys-403 tematic design procedure proposed in this work. The final dimensions (in mm) of the 404 filter (obtained in a low-precision space) are: $H_1 = H_5 = 22.960, H_2 = H_4 = 20.099,$ 405 $H_3 = 20.069, s_{1,2} = s_{4,5} = 22.198, s_{2,3} = s_{3,4} = 28.463 \text{ and } d = 4.382.$ 406



Figure 15. S-parameters of the 5th-order interdigital filter (coarse model) and response of the coarse model filter in the high-precision space (label: initial point).

5.4 Implementation of the ASM Technique

407

As already mentioned, all previous simulations have been performed in a low-accuracy space (using FEST3D). To continue, therefore, the final dimensions obtained in the previous section need to be mapped to a high-precision space using the ASM method. In this context, we have included in Fig. 15 the filter response in the high-precision space using the optimum dimensions designed in the coarse space.

Fig. 16 shows the frequency response of the filter after implementing the ASM tech-413 nique. Again, two different EM simulators (Ansys HFSS and CST Studio Suite) have 414 been used to validate the design process, obtaining an excellent agreement between both 415 set of simulated data. In addition, the electrical response of the filter designed in the low-416 accuracy simulation space has also been included in Fig. 16. The values (in mm) of the 417 dimensions of the 5th-order interdigital filter (after implementing the ASM technique) 418 are: $H_1 = H_5 = 23.100, H_2 = H_4 = 20.204, H_3 = 20.174, s_{1,2} = s_{4,5} = 21.839, s_{2,3} = s_{3,4} = 3.100$ 419 28.059 and d = 4.421. 420

Finally, we have compared in Table 1 the electrical performance of the bandpass filters designed in this work (3rd and 5th-order filters) with other similar designs (found in the technical literature) concerning interdigital waveguide bandpass filters using resonator posts with a cylindrical or a rectangular geometry.

⁴²⁵ 6 Multipactor breakdown prediction

A power handling capability study of the designed interdigital filters is addressed 426 in this section. In particular, the high-power performance of both topologies of interdig-427 ital filters discussed in this work (based on cylindrical posts and on flat strips) will be 428 compared. The multipactor effect is a high-power phenomenon that appears in compo-429 nents used in communication satellites, under high vacuum conditions and in the pres-430 ence of high-intensity electromagnetic fields, linked to an electron avalanche effect (Vaughan, 431 1988). This phenomenon can lead to a degradation of the device performance, so it is 432 very important to properly characterize the behaviour of the designed components un-433 der high-power conditions. 434

In this context, Fig. 17 shows the electric field distribution in the 5th-order interdigital filter based on flat strips computed at $f_0=3$ GHz (with values scaled for an in-



Figure 16. S-parameters of the 5th-order interdigital bandpass filter in the high-precision space. Comparison of results obtained with Ansys HFSS and CST Studio Suite.

Table 1. Electrical performance of several interdigital waveguide bandpass filters found in the technical literature.

Ref.	$f_0 (\text{GHz})$	N	BW (GHz)	RL (dB)	Post geometry
This work	3	3	0.2	25	Rect.
This work	3	5	0.2	25	Rect.
(Packiaraj et al., 2005)	0.975 - 1.825	3	$0.25 \ / \ 0.35$	15	Cyl.
(Ikram & Rana, 2006)	6.175	5	0.5	10	Cyl.
(Munina & Turalchuk, 2015)	2.91 - 3 - 3.09	3	$\simeq 0.04 - 0.04$ - 0.04	20	Cyl.
(J. Li et al., 2018)	15	8	4.4	10	Cyl.
(Wu et al., 2019)	14	4	1.4	15	Rect.
(Jiang et al., 2019)	11.725	8	2.05	17	Rect.
(Rodriguez-Morales et al., 2021)	3.75	11	2	10	Rect.
(Rodriguez-Morales et al., 2021)	6	11	2	10	Rect.
(Kong et al., 2023)	3.8	4	0.9	18	Rect.

put power level of 1 W). The electric field distribution reveals a high concentration of 437 the electric field around all the metallic strips. Typically, the critical areas in terms of 438 multipactor effect for classical interdigital resonators based on cylindrical posts are the 439 zones between the top surface of the post and the top/bottom walls of the rectangular 440 enclosure. Nevertheless, for the novel resonators based on planar strips proposed in this 441 work, since the thickness of the strip used in our designs is small (only 1 mm), the equiv-442 alent capacitance in this region is less significant than the one found in classical resonators 443 based on cylindrical posts. Therefore, a multipactor analysis in several isolated regions 444 of the designed filters is required to identify the critical zones in this new filter topol-445 ogy. 446

After analysing the evolution of the electrons trajectory in the designed filters, we 447 have identified that the critical areas in these structures are the flat surfaces of the first 448 and last resonator strips facing the front and back walls of the rectangular enclosure (where 449 the distance is of 3 mm). In these zones, there is, indeed, a large capacitance (probably 450 the largest in the whole structure), thus becoming the most critical regions in terms of 451 the multipactor phenomenon. This fact has to be taken into account if these filters are 452 to be used in space applications, since, under vacuum conditions, they will be suscep-453 tible to resonant electron discharges. 454

Next, a power analysis of the interdigital filters designed in this work (considering 455 that they have been manufactured in aluminium) has been performed under vacuum con-456 ditions using the commercial software Spark3D (which is part of CST Studio Suite). To 457 do this, we have first used Ansys HFSS to compute the EM fields at the central frequency 458 of the designed filters $(f_0=3 \text{ GHz in all cases})$, and also at the frequencies $(f_1 \text{ and } f_2)$ 459 where the S_{21} parameter group delay and stored energy are maximum. Next, the cal-460 culated EM fields are imported by the Spark3D simulator, which is used to estimate the 461 multipactor power threshold (P_{th}) of the designed filters. A homogeneous electron seed-462 ing of 10000 initial electrons has been defined in the simulations. In addition, the main 463 parameters of the SEY curve are: $\delta_{\text{max}} = 2.92, \delta_0 = 0.8, E_1 = 17 \text{ eV}$ and $E_{max} = 276$ eV (ESA-ESTEC, E. P. D., 2020). 465

The obtained results for the 3rd-order interdigital filter based on flat strips are $(f_1 =$ 466 2.86 GHz, $f_2 = 3.15$ GHz): $P_{th,f_0} = 170$ W, $P_{th,f_1} = 72.8$ W and $P_{th,f_2} = 83.5$ W. 467 Moreover, for the 5th-order interdigital filter we have obtained $(f_1 = 2.91 \text{ GHz}, f_2 =$ 468 3.09 GHz): $P_{th,f_0} = 100$ W, $P_{th,f_1} = 45.4$ W and $P_{th,f_2} = 51.3$ W. Although the obtained multipactor power thresholds are lower at frequencies f_1 and f_2 , in practice, the 470 frequency bandwidth of the employed signals do not usually reach such extreme values. 471 The minimum of these computed P_{th} values would be the maximum operating power of 472 each filter in space applications. If needed, solutions like the one proposed in (Coves et 473 al., 2023) can be used to increase these values. 474

In order to compare the power handling capability of the new proposed topology 475 with that of the classical solution based on cylindrical posts, a multipactor analysis has 476 also been performed for the designed 3rd-order interdigital filter based on cylindrical res-477 onators. The obtained results are $(f_1 = 2.83 \text{ GHz}, f_2 = 3.17 \text{ GHz})$: $P_{th, f_0} = 79.4 \text{ W}$, 478 $P_{th,f_1} = 40.9$ W and $P_{th,f_2} = 31.4$ W. Therefore, compared to the data obtained for 479 the 3rd-order filter based on flat strips, we can conclude that the new proposed topol-480 ogy exhibits a better high-power performance than the classical interdigital filters based 481 on cylindrical resonators. 482

483 7 Conclusion

A systematic procedure for the efficient design of a new topology for interdigital bandpass filters, based on flat metallic strips, has been proposed. The design method combines the use of the classical circuit-based approach and a strategy based on the seg-



Figure 17. Electric field ($f_0 = 3 \text{ GHz}$) in the 5th-order interdigital bandpass filter.

mentation of the filter, with the aim of reducing the number of variables to be optimized 487 at each stage of the design process. Moreover, the ASM technique has been used in or-488 der to perform most of the simulations in a low-accuracy space, thus reducing the over-489 all computational effort. Two interdigital bandpass filters operating in the S-band have 490 been designed, and their electrical responses have been successfully compared to the re-491 sults provided by two different EM full-wave simulators, thus validating both the new 492 topology and the design procedure proposed. In addition, a multipactor study has been 493 performed, in order to characterize the power capability of the components under vac-494 uum conditions, in view of a possible use of the designed filters in satellite payloads. Fi-495 nally, the design of a 3rd-order interdigital filter based on cylindrical posts has also been discussed. Our results have shown that the topology based on flat strips is as compact 497 as the classical topology based on cylindrical post resonators, while exhibiting an enhanced 498 broadband performance and a better power handling capability. 499

500 Open Research Section

Data were not used nor created for this research. The simulation results were obtained using ANSYS High Frequency Structure Simulator (ANSYS, 2024) and CST Studio Suite (Dassault Systemes, 2024).

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