On the Capacity Gain of Multi-Hop Cellular Networks with Opportunistic Networking and D2D: a Space-Time Graph-based Evaluation

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Abstract—Previous studies have shown that device-centric wireless technologies, including multi-hop cellular networks (MCNs) and device-to-device (D2D) communications, can increase the cellular network capacity. This study focuses on 2-hop uplink MCN communications, where source nodes (S) need to upload a message of size $F$ to the cellular base station (BS) before a deadline of $T$. To do so, S must first establish a D2D link with a mobile relay (R) that will then upload the information to the BS. This study considers that a D2D link can be established when devices are within a radio range $r_{D2D}$ and under line-of-sight (LOS). This ensures stable and high-throughput D2D links. This study considers the use of efficiency-driven opportunistic networking in the D2D and cellular links. In this case, opportunistic networking is utilized to search for and establish efficient D2D and cellular links, and not to handle disconnections. An efficient link is here defined as a link that reduces the cellular transmission time of a MCN connection, and hence increases the cellular network capacity. Other criteria could be considered.

Opportunistic networking has been commonly studied using graph theory as it provides the necessary tools to model the (pairwise) relations between nodes and their contact opportunities. Different types of network graphs can be used to represent the connectivity among mobile nodes [4]. Wireless graphs are time-varying graphs where edges between nodes indicate the presence of a wireless link. Wireless graphs are only modified when nodes move out of their communications range. Contact graphs are created by aggregating statistics from the dynamic wireless graphs (e.g. contact frequency or duration, or inter-contact time). Social graphs can partly solve the tractability problems of contacts graphs with a high number of nodes by defining sub-graphs (or communities) based on the social relations between nodes. All these graphs have been commonly utilized for networks that suffer disconnections, and increase the QoS, and offload cellular traffic. This study extends the current state of the art by investigating the upper-bound system capacity gains that the integration of opportunistic networking and MCNs (referred to as opportunistic MCN in this paper) could provide over conventional cellular networks. To this aim, this paper proposes to model opportunistic MCN with space-time graphs, and defines an optimization framework to identify the configuration of opportunistic MCN that maximizes the capacity gains compared to conventional single-hop cellular networks.

II. SPACE-TIME GRAPH MODEL

This study focuses on 2-hop uplink MCN communications, where source nodes (S) need to upload a message of size $F$ to the cellular base station (BS) before a deadline of $T$. To do so, S must first establish a D2D link with a mobile relay (R) that will then upload the information to the BS. This study considers that a D2D link can be established when devices are within a radio range $r_{D2D}$ and under line-of-sight (LOS). This ensures stable and high-throughput D2D links. This study considers the use of efficiency-driven opportunistic networking in the D2D and cellular links. In this case, opportunistic networking is utilized to search for and establish efficient D2D and cellular links, and not to handle disconnections. An efficient link is here defined as a link that reduces the cellular transmission time of a MCN connection, and hence increases the cellular network capacity. Other criteria could be considered.

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assuming that a link is established as soon as two nodes get in contact with each other. This study considers a network without disconnections since all devices are always under cellular coverage. In this case, opportunistic networking is here utilized for establishing links between nodes, and between nodes and the infrastructure, when the most efficient transmission conditions are met. This study proposes to model these opportunistic MCN connections using space-time graphs. Space-time graphs create a dynamic sequence of graphs in order to represent the time evolution of the nodes’ location and connectivity. Each graph represents a snapshot of the network topology, and it is assumed that the network conditions remain unchanged between snapshots. The snapshots are created every $\Delta t$ seconds in order to search for the conditions where efficiency-driven opportunistic networking can establish D2D and cellular links that minimize the cellular transmission time.

This study models 2-hop uplink MCNs as a sequence of graphs $G = \{G_{t1}, G_{t2}, \ldots, G_{tT}\}$ where $G_{t}$ is the graph representing the network at time $t$, $V_{t} = \{S, R_{1}, R_{2}, \ldots, R_{n}\}$ denotes the nodes of the graph, and $E_{t}$ represents the presence of a $S$-$R_i$ D2D link when $D2D$ and cellular transmissions actually take place when $D2D$ and cellular transmissions actually take place between $S$ and $R_i$, and between $R_i$ and the $BS$. The constructed space-time graph models all possible D2D and cellular links in order to identify the ones that minimize the cellular transmission time, and hence result in the largest capacity gain. To this aim, we propose the following optimization framework:

$$\begin{align*}
\alpha, \beta : \min \{N_{R_i}\} & = \min \left( \sum_{x \in \Delta t} C_{x}(R, S) \right) \\
\text{s.t.:} & \quad \sum_{x \in \Delta t} d_{x}(S, R) = \frac{\sum_{t=2}^{T} t_{D2D}}{\Delta t} \\
\text{and} & \quad \sum_{x \in \Delta t} c_{x}(R, S) \cdot \Delta t \leq 2 \Delta t 
\end{align*} \tag{1}$$

where $N_{R_i}$ represents the cellular transmission time from $R_i$ to the $BS$. $d_{x}(S, R)$ and $c_{x}(R, S)$ are binary variables used to indicate when D2D and cellular transmissions actually take place between $S$ and $R_i$, and between $R_i$ and the $BS$, respectively. The variables are equal to one when the transmission takes place, and equal to zero otherwise. The D2D transmissions can only take place when $S$ and $R_i$ are under LOS and at a distance smaller than $r_{D2D}$.

The objective function (1) is subject to a set of constraints. Constraint (2) ensures that the selected mobile relay $R_i$ has a D2D link with $S$ at least for $t_{D2D}$ seconds (or during $t_{D2D}/\Delta t$ events in the space-time graph; these events do not need to be consecutive in time as opportunistic networking is integrated with D2D). $t_{D2D}$ represents the duration of the D2D transmission from $S$ to $R_i$. Constraint (3) ensures that the message of size $F$ is completely transmitted from $R_i$ to the $BS$ before $T$. $thr_{R_i}(x)$ represents the uplink cellular throughput experienced by $R_i$ at time instant $x$. Constraint (4) guarantees that the $(R_i, BS)$ cellular link does not transmit more information than what is received through the $(S, R_i)$ D2D link. $I$ represents the data transmitted in the D2D link during $\Delta t$ (i.e. $I = \Delta t/F_{\text{D2D}}$).

The optimization framework is executed for all mobile devices which have been in contact with $S$ (i.e. $\forall R_i \in R$) during...
The evaluation environment follows 3GPP guidelines and models for the simulation of outdoor urban scenarios (3GPP TR36.873 and [6]). The study considers a Manhattan-like scenario with \{5x5, 8x8, 11x11\} blocks. The width of buildings and streets is set equal to 89m and 11m respectively. These settings are selected to analyze the performance under various heterogeneous outdoor deployments characteristic of urban environments. The BS is located at the center of the scenario, and provides coverage to the complete scenario. The cell radius is then equal to \(350, 560, 770\)m for these scenarios respectively. Mobile devices are uniformly distributed, and move at 2 m/s. At intersections, the devices have the same probability of turning right, left or continue straight. Different densities of nodes have been modelled following the guidelines in [6] for the test case “dense urban information society (duis)”. The spatial density of mobile devices (\(\lambda\)) within a cell has been set equal to \(\{0.25, 0.5\}\) \(\lambda_{\text{duis}}^2\). \(\lambda_{\text{duis}}\) is the spatial density of pedestrians in [6], and is equal to \(8.500\) users/km\(^2\). The study does not focus on any particular traffic service, but considers that source nodes need to upload a file of size \(F=100\times\text{MB}\) before a deadline \(T=30, 100, 220\)s. \(T\) 30, 100 and 220s correspond to the time conventional single-hop cellular communications need to complete the transmission of \(F\) at the border of cells with \(350, 560, 770\)m radius respectively.

The cellular connection to the BS is an LTE connection at 2GHz. The system bandwidth is set to 10MHz, and the cellular transmissions utilize 6 physical resource blocks. The cellular propagation losses are modelled using the 3D urban macro-cellular (3D-UMa) channel model reported in 3GPP TR36.873. Log-normal fading with standard deviation \(\sigma_G=4\) dB (LOS) and \(\sigma_F=6\) dB (NLOS) is also included. The LTE uplink throughput is estimated using the SNR-BER curves reported in [7] for different CQIs (the target BER is 0.1), and the tables in 3GPP TS36.213 that map CQI values and transmission modes to the associated transport block index \((i_{\text{TBs}})\). \(i_{\text{TBs}}\) varies from 0 to 26 with the highest values associated to the highest transmission modes (i.e. the combinations of modulation and coding schemes resulting in the highest data rates) and larger transport block sizes.

\(S\) communicates with \(R\) using 802.11g at 2.4GHz. 3GPP considers both 802.11 and LTE for D2D (or sidelink as referred to in 3GPP) communications. The empirical measurements in [8] showed that 802.11g uses its highest data rate (54Mbps) up to a maximum distance of 80m under LOS. \(t_{\text{D2D}}\) has then been set equal to 80m in this study. Radio transmission errors and medium access overhead (or channel efficiency as defined in [8]) result in an 802.11g throughput that varies between 15 and 30Mbps for distances up to 80m under LOS when using the 54Mbps data rate. We assume the worst-case scenario, and consider that all D2D transmissions experience a 15Mbps throughput. The time needed to transmit a file of size \(F=30\text{MB}\) at 15Mbps over a D2D link \(t_{\text{D2D}}\) has hence been set to 2s.

The scenario is simulated in Matlab. \(At\) is set equal to 1s as a compromise between tractability and accuracy. A minimum of 10,000 experiments have been conducted for each combination of parameters to guarantee that the standard error of the mean is below 0.5%. A user \(S\) within the cell is randomly selected in each experiment to solve the optimization framework (1)-(6) using exhaustive search. The performance experienced by \(S\) using opportunistic MCN is compared against that experienced by \(S\) (same position and time instant) using conventional single-hop cellular communications where \(S\) directly transmits the information to the BS (SH mode). To this aim, we obtain a value of \(N\) (using (6)) and \(N_S\) for each experiment. \(N_S\) is the cellular transmission time needed by \(S\) to upload the file using the SH mode. In this mode, the cellular transmission from \(S\) to the BS starts at time instant \(At\) and cannot be paused. We then compute \(\gamma\) that represents the average percentage reduction of the cellular transmission time that opportunistic MCN achieves with respect to the SH mode. \(\gamma\) is computed as the average value of \(100\% (1 - N/N_S)\) over all the experiments conducted for each combination of parameters. The capacity gain is computed as \(100\% (\gamma/(100\% - \gamma))\), and represents how many more opportunistic MCN transmissions than SH ones can be served with the same cellular channel occupancy.

V. CAPACITY ANALYSIS

The proposed space-time graph and optimization framework are utilized in this section to identify the upper-bound of the capacity gains that can be obtained with the utilization of opportunistic MCN. Fig. 2 shows the average capacity gain (in %) that opportunistic MCN can achieve with respect to SH. Fig. 2 shows that the minimum capacity gain for all scenarios is 36.8% (cell radius=350m, \(T=30s\)); this corresponds to a reduction of the cellular transmission time of 26.9%.

![Fig. 2. Capacity gain (\(\lambda=0.5\lambda_{\text{duis}}\)).](image)

Fig. 2 shows that the capacity gains obtained with opportunistic MCN augment with \(T\) and the cell size. For example, opportunistic MCN increases the capacity by 47.1%
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when $T$ is equal to 30s and the cell size is 560m. The capacity gain augments to 143.9% when $T$ is set equal to 220s. As the service deadline $T$ increases, opportunistic MCN can find better combinations of D2D and cellular links to reduce the cellular transmission time. The cell size has also a significant impact. Larger cell sizes degrade the QoS of conventional single-hop cellular communications, in particular for users far away from the BS. These users significantly benefit from opportunistic MCN that considerably improves their link budget. For example, opportunistic MCN increases the capacity by 45.7% when the cell size is 350m and $T$ is equal to 220s. The capacity increases by 273.1% when the cell size augments to 770m. The results reported in Fig. 2 correspond to average values across the cell area. The impact of opportunistic MCN augments when the source node is not close to the BS (in particular, at distances higher than 150m). For example, opportunistic MCN reduces the cellular transmission time by 20% when the source node is 250m away from the BS ($T=220s$, cell size=770m). This value augments to 82% when the source node is 550m away from the BS. Similar trends as those reported in Fig. 2 have been observed for lower spatial densities of nodes, in particular for $\lambda=0.25\cdot\lambda_{diss}$. However, the benefits of opportunistic MCN augment with $\lambda$ because of the higher contact opportunities between nodes. The impact of $\lambda$ reduces when $T$ increases.

Opportunistic MCN can reduce the cellular transmission time since it is able to identify favorable communication conditions under which to perform the D2D and cellular transmissions. In the conducted evaluations, the cellular transmissions within opportunistic MCN connections always experienced higher CQI levels than SH. High CQI values are associated to high modulation and coding schemes, and consequently higher throughput levels. For example, 99% of the cellular transmissions within opportunistic MCN connections experienced the highest CQI levels when $T=100s$ and the cell radius was equal to 350m. This value decreased to only 18% for the SH mode.

Fig. 3 compares the capacity gain achieved with opportunistic MCN (‘Opp-MCN’ in Fig. 3) to that obtained with other communication modes. The opportunistic cellular mode (‘Opp-cellular’ in Fig. 3) refers to the case in which source nodes do not use mobile relays, and directly transmit the information to the BS using a cellular connection that integrates the efficiency-driven opportunistic networking paradigm. In the MCN mode, $S$ transmits the information to the BS using a MCN connection that does not utilize opportunistic networking at the D2D and cellular links. Similarly to the opportunistic MCN mode, the selected mobile relay has to be in LOS conditions with $S$ and within a radio range $r_{D2D}$. The MCN mode requires selecting the mobile relay at time $\Delta t$, and starting the cellular transmissions from the selected mobile relay to the BS at time $2\Delta t$. For a fair comparison with the opportunistic MCN mode, we have designed optimization processes similar to that reported in (1)-(6) for the opportunistic cellular and MCN modes. These processes have been adapted to the characteristics of these two modes, but also seek to identify the time instants at which the cellular transmissions should take place in order to minimize the cellular transmission time. In particular, the optimization framework defined for the opportunistic cellular mode includes equations (1) and (3) with $x \in [1, M, T, \Delta t]$ for $c_{x(S,BS)}$, but does not include the term $d_{x(S,BS)}$ as the mode does not utilize D2D transmissions. The optimization framework for the MCN mode includes the equations (1)-(4) with $x \in [T, \Delta t, 2\Delta t]$ for $d_{x(S,Ri)}$, and an additional constraint ($\sum_{x=1}^{T} t_{ht}(x) - \Delta t > \sum_{x=1}^{T} t_{ht}(x) - \Delta t$, $\forall x \in [2\Delta t, T, \Delta t]$), to indicate that the cellular transmissions from the selected mobile relay to the BS have to start at $2\Delta t$ and cannot be paused. Using their respective frameworks, we also derive the minimum cellular transmission times ($N$) for the opportunistic cellular and MCN modes (following eq. (6)), and compute their capacity gains with respect to the SH mode following the same procedure as defined for the opportunistic MCN mode. Fig. 3 demonstrates that the large capacity gains achieved by opportunistic MCN result from the combined use of opportunistic networking and MCN.

This study has investigated the capacity gains that can be obtained from the utilization of opportunistic networking and MCN. To do so, the study models opportunistic MCN connections using a space-time graph, and proposes an optimization framework for minimizing the cellular transmission time. The results show that opportunistic MCN can significantly increase the cellular capacity (by up to 273% under the evaluated conditions). The gains are particularly relevant as the cell size or service deadline increase. Opportunistic MCN can increase the capacity without modifying the radio interface, and the increase is not constrained to any radio interface. This paves the new way for further gains as new 5G radio interfaces are introduced.

VI. CONCLUSIONS

References