

# Analysis of Multipactor Effect in a Partially Dielectric-Loaded Rectangular Waveguide

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**Abstract**—This paper presents a study of the multipactor effect in a partially dielectric-loaded rectangular waveguide. To obtain the simulations presented in this paper, a detailed analysis of the dynamics of the electron inside this waveguide has been performed, taking into account the radio frequency electromagnetic fields propagating in the waveguide and the dc electric field that appears because of the charging of the dielectric layer. This electrostatic field is obtained by computing the electric potential produced by an arbitrary charge distribution on the dielectric layer in a dielectric-loaded waveguide. The electron trajectory is then found by numerically solving the equations of motion. The results obtained show that multipactor discharges do turn off by themselves under certain circumstances when they occur in such dielectric-loaded waveguide.

**Index Terms**—Multipactor, secondary emission, waveguide.

## I. INTRODUCTION

MULTIPACTOR is a high-power resonant electron discharge frequently observed in the microwave and millimeter-wave subsystems operating under vacuum conditions [1] present in a wide range of different scenarios, such as passive components of satellite communication payloads, traveling-wave, tubes or particle accelerators. In an ultrahigh vacuum environment, the free electrons inside a microwave device are accelerated by the radio frequency (RF) electromagnetic fields, impacting against its metallic walls. If the electron impact energy is high enough, one or more secondary electrons might be released from the surface. When some resonance conditions are satisfied, the secondary electrons get synchronized with the RF fields, and the electron population inside the device grows exponentially leading to a multipactor discharge. This multipactor discharge has some negative effects that degrade the device performance: increase

of signal noise and reflected power, heating of the device walls, outgassing, detuning of resonant cavities, and even the partial or total destruction of the component.

Multipactor research lines are aimed to study and characterize the phenomenon to predict the conditions for its appearance [2], [3]. Some RF devices, such as filters, multiplexers, and RF satellite payloads, include dielectric materials commonly employed as resonators and supporting elements. In [4], it is presented a review of multipactor discharge on metals and dielectric windows that takes into account the surface materials, and the effects of space charge and cavity loading. The multipactor effect including the presence of dielectric materials in single-surface multipactor regime has been widely investigated in the context of particle accelerators; for instance, in ceramic RF windows [5], [6] and in alumina-based dielectric-loaded accelerating structures [7]. In contrast, very few contributions can be found about multipactor breakdown on dielectrics in the scenario of RF systems for space applications [8]–[10], and mostly under the parallel-plate waveguide approximation. In [11] and [12], the effective electron model (EEM) has been successfully used for simulations of multipaction experiments in coaxial transmission lines considering the presence of external magnetic static fields, demonstrating the validity of this method in complex scenarios. The multipactor inside an empty rectangular waveguide has also been studied in [13] and [14], where the conventional resonance theory gives correct predictions for the multipactor threshold if the height of the waveguide is very small and first-order resonance multipactor dominates. When the waveguide height exceeds a certain critical value, which depends on the waveguide width, an accurate prediction of the multipactor threshold requires considering the RF fields inside the waveguide without approximations. Therefore, there is a need to accurately predict the electron discharge on devices involving partially dielectric-loaded rectangular waveguides, which are of more practical interest for satellite technology. The main aim of this investigation is to extend the results of previous works [8]–[10], where an EEM was successfully applied to study the multipactor in a parallel-plate dielectric-loaded waveguide, to the analysis of multipactor effect in a partially dielectric-loaded rectangular waveguide.

In Section II, the theoretical model employed for the simulations is discussed. In Section III, the multipactor prediction results of an empty rectangular waveguide are analyzed and compared with results from the technical literature for validation purposes. Then, the susceptibility chart of a partially

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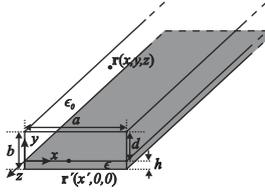


Fig. 1. Geometry and dimensions of the problem under investigation.

monomode regime, where only the fundamental mode,  $\text{TM}_{10}^y$ , propagates in the waveguide. The instantaneous field vectors interacting with the effective electron are given by

$$\mathbf{E}_{\text{RF}}(x, y, z, t) = E_0 \Re\{\mathbf{e}(x, y) e^{j(\omega t - \beta z + \varphi_0)}\} \quad (1a)$$

$$\mathbf{H}_{\text{RF}}(x, y, z, t) = H_0 \Re\{\mathbf{h}(x, y) e^{j(\omega t - \beta z + \varphi_0)}\} \quad (1b)$$

where  $\varphi_0$  is the initial phase and  $E_0, H_0$  are the constants related to the transmitted power in the waveguide. The modal fields  $\mathbf{e}(x, y)$  and  $\mathbf{h}(x, y)$  and the propagation constant  $\beta$  of the  $\text{TM}_{10}^y$  mode can be found in [18] and [19]. These expressions can be directly extended if higher order modes must be taken into account (i.e., in waveguide discontinuities) by using the mode-matching technique.

The key to understanding the mechanism of a multipactor discharge is to study the behavior of the electrons within the waveguide, which are accelerated by the aforementioned electromagnetic fields  $\mathbf{E}_{\text{RF}}$  and  $\mathbf{H}_{\text{RF}}$ . In this way, sooner or later, these fields will make an electron impact with any surface of the rectangular waveguide, which can result in the emission or absorption of secondary electrons. If the impacts occur on the dielectric surface, unlike the case of impacts on the metallic walls, the secondary electrons emitted by the dielectric give rise to positive charges at the impact positions on the dielectric surface, while the electrons absorbed in the dielectric layer will generate negative charges in it. These charges, which are located on the dielectric surface at positions  $\mathbf{r}' = (x', 0, z')$ , give rise to an electrostatic field  $\mathbf{E}_{\text{dc}}$ , which has to be added to the RF fields to obtain accurately the trajectory of the electrons inside the waveguide. In order to determine the electrostatic field,  $\mathbf{E}_{\text{dc}}(x, y, z) = -\nabla\phi(x, y, z)$ , generated by the charges on the dielectric, the potential  $\phi(x, y, z)$  inside the waveguide has to be first calculated. Using the superposition, the potential in the waveguide due to the set of charges  $Q_i$  on the dielectric surface can be obtained by adding the individual contribution of each charge

$$\phi(x, y, z) = \sum_i G(x - x'_i, y, |z - z'_i|) Q_i(x'_i, 0, z'_i) \quad (2)$$

where  $G(x, y, z)$  is the electrostatic potential due to a unit point charge, that is, Green's function for this problem.

The above-mentioned Green's function,  $G(x, y, z)$ , is the solution to the following Laplace's equation [20], [21]:

$$\nabla \cdot [\epsilon_r(y) \nabla G(x, y, z)] = -\frac{1}{\epsilon_0} \delta(x - x') \delta(y) \delta(z) \quad (3)$$

where  $\epsilon_0$  is the free-space dielectric permittivity and the position of the unit charge is taken at  $(x', 0, 0)$  for convenience. Both the geometric characteristics and the linear nature of the problem under consideration makes that the Dirac delta functions can be expressed as [21]

$$\delta(x - x') = \frac{2}{a} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') \quad (4)$$

$$\delta(z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-jk_z z} dk_z \quad (5)$$

where  $k_{xn} = n\pi/a$  and  $k_z$  is the spectral Fourier variable along the longitudinal direction  $z$ . The above-mentioned expressions

79 dielectric-loaded rectangular waveguide is obtained with the  
80 developed model, and the time evolution of a discharge in  
81 this waveguide is studied and discussed. Finally, Section IV  
82 outlines the main conclusions of this paper.

## 83 II. THEORY

### 84 A. Computation of RF and DC Fields in a Partially 85 Dielectric-Loaded Waveguide

86 Fig. 1 shows the scheme of a partially dielectric-loaded  
87 rectangular waveguide of width  $a$  and height  $b$ , and whose  
88 dielectric material has relative permittivity  $\epsilon_r$ . In the problem  
89 under study, the dielectric slab of thickness  $h$  and width  $a$  is  
90 placed over the bottom waveguide wall, being  $d$  the empty  
91 waveguide height where the effective electron travels (see  
92 Fig. 1). The RF electromagnetic field is assumed to propagate  
93 along the positive direction of the  $z$ -axis. For the sake of  
94 simplicity, the waveguide is supposed to be infinite along the  
95  $z$  direction, and a time-harmonic dependence of the type  $e^{j\omega t}$   
96 is implicitly assumed, with  $f = \omega/2\pi$  being the frequency  
97 and  $t$  the time measured in the laboratory reference sys-  
98 tem. To analyze the multipactor evolution in this waveguide,  
99 a multipactor simulation code based on the Monte Carlo  
100 method has been developed. The software code, similar to the  
101 one described in [8] and [9], employs the single EEM [15].  
102 This assumption avoids the consideration of space-charge  
103 effects, what is a strong simplification. The space-charge  
104 effects are often neglected in the analysis of the first stages of  
105 the multipactor discharge [13], [14], but they are doubtless  
106 important at high electron populations when the discharge  
107 is fully developed. Simulation results of some published  
108 works [16], [17] indicate an important role of space-charge in  
109 the evolution of the multipactor process to a saturation stage.  
110 In this paper, however, we are mainly interested in studying  
111 the influence of dielectric charging in the multipactor process.  
112 The inclusion of space-charge effects, although providing a  
113 more realistic description of the global process, would increase  
114 the computational burden very much, as the dc field due  
115 to dielectric charging has to be evaluated in every effective  
116 electron position. In addition, the interpretation of simulation  
117 results would become difficult, as dielectric charging and space  
118 charge can both lead to a repulsion of the freshly emitted  
119 secondary electrons back to the surface.

120 The effective electron at  $\mathbf{r} = (x, y, z)$  can move in the  
121 air region of height  $d$  of the rectangular waveguide. The  
122 electromagnetic fields  $\mathbf{E}_{\text{RF}}$  and  $\mathbf{H}_{\text{RF}}$  acting on the effective  
123 electron correspond to the modes of the partially dielectric-  
124 loaded rectangular waveguide (Fig. 1), which are hybrid modes  
125 of  $\text{TM}^y$  and  $\text{TE}^y$  kinds [18]. We have restricted our study to the

175 come from the fact that the eigenfunctions of the differential  
176 operator are sinusoidal functions along  $x$ -axis and complex  
177 exponential functions along the  $z$ -axis, respectively. This is  
178 equivalent to apply the discrete sine transform along the  $x$ -axis  
179 and the integral transform along the  $z$ -axis, namely,

$$180 \quad G = \frac{1}{\pi a} \int_{-\infty}^{\infty} dk_z e^{-jk_z z} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') \tilde{G} \quad (6)$$

$$181 \quad \tilde{G} = \int_{-\infty}^{\infty} dz e^{jk_z z} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') G \quad (7)$$

182 where  $G = G(x, x', y, z)$  and  $\tilde{G} = \tilde{G}(k_{xn}, k_z; y)$ .

183 According to the above-mentioned considerations, (3) can  
184 be expressed as the following ordinary differential equation  
185 for the spectral Green's function  $\tilde{G}$ :

$$186 \quad \left\{ \frac{d}{dy} \epsilon_r(y) \frac{d}{dy} - k_t^2 \right\} \tilde{G} = -\frac{\delta(y)}{\epsilon_0} \quad (8a)$$

$$187 \quad \tilde{G}(y = -h) = 0 \quad (8b)$$

$$188 \quad \tilde{G}(y = d) = 0 \quad (8c)$$

189 where  $k_t^2 = k_{xn}^2 + k_z^2$ . Solving (8), the following expression  
190 for  $\tilde{G}$  is obtained in the air region  $y \geq 0$ :

$$191 \quad \tilde{G}(k_{xn}, k_z; y) = \frac{\sinh[k_t(d - y)]}{\epsilon_0 k_t [\epsilon_r \coth(k_t h) + \coth(k_t d)] \sinh(k_t d)}. \quad (9)$$

193 Green's function in the spatial domain,  $G$ , is achieved by  
194 replacing (9) into (6) to give

$$195 \quad G(x, x', y, z) \\ 196 \quad = \frac{2}{\epsilon_0 \pi a} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') \\ 197 \quad \times \int_0^{\infty} \frac{\sinh[k_t(d - y)] \cos(k_z z)}{k_t [\epsilon_r \coth(k_t h) + \coth(k_t d)] \sinh(k_t d)} dk_z. \quad (10)$$

198 In (10), if the point charge is placed at  $z' \neq 0$ ,  $z$  must  
199 be replaced by  $(z - z')$ . Here, it is worth noting that very  
200 efficient numerical summation and integration techniques have  
201 to be employed to compute Green's function with sufficient  
202 accuracy and tolerable CPU times [22].

203 Once Green's function has been calculated, the  $\mathbf{E}_{dc}$  field is  
204 obtained by numerical differentiation of (2) by means of the  
205 central difference technique.

### 206 *B. Multipactor Evolution in the Partially* 207 *Dielectric-Loaded Waveguide*

208 Once the RF and dc fields are known at any instant  $t$ ,  
209 the electron dynamics inside the waveguide can be computed,  
210 which is governed by the Lorentz force and related to its linear  
211 momentum

$$212 \quad \mathbf{F}_L = q(\mathbf{E} + \mathbf{v} \times \mathbf{B}) = \frac{d\mathbf{p}}{dt} \quad (11)$$

213 where  $q = -e$  is the electron charge,  $\mathbf{E}$  and  $\mathbf{B} = \mu_0 \mathbf{H}$   
214 are the total electric and magnetic fields (both RF and dc

215 contributions) interacting with the electron,  $\mu_0$  is the free-  
216 space magnetic permeability, and  $\mathbf{v}$  is the velocity vector of  
217 the electron. The linear relativistic momentum is defined as

$$218 \quad \mathbf{p} = m_0 \gamma \mathbf{v} \quad (12)$$

219 where  $m_0$  is the electron rest mass,  $\gamma = 1/\sqrt{1 - (v/c)^2}$  the  
220 Lorentz factor,  $v$  is the magnitude of the velocity vector, and  
221  $c = 1/\sqrt{\mu_0 \epsilon_0}$  the speed of light in vacuum. Although the  
222 relativistic correction in this equation can be discarded for the  
223 typical power ranges of most space waveguide devices, it must  
224 be considered when high velocities are reached ( $v/c \geq 0.1$ ),  
225 as in high-power multipactor simulations. Expanding (11),  
226 the following differential equation is obtained:

$$227 \quad -\mathbf{E} - \mathbf{v} \times \mathbf{B} = M \gamma \mathbf{a} + \frac{M}{c^2} \gamma^3 (\mathbf{v} \cdot \mathbf{a}) \mathbf{v} \quad (13)$$

228 where  $\mathbf{a}$  is the acceleration vector and  $M = m_0/e$ . The  
229 differential equation to be solved becomes

$$230 \quad \ddot{\mathbf{r}} = \frac{-\dot{\mathbf{r}} \times \mathbf{B} - \mathbf{E} + \dot{\mathbf{r}} \cdot (\dot{\mathbf{r}} \cdot \mathbf{E})/c^2}{M \gamma}. \quad (14)$$

231 The electron trajectory is found by numerically solving  
232 the above-mentioned equations of motion. For that purpose,  
233 a Velocity Verlet algorithm [23] has been used, which assures  
234 sufficient accuracy and good efficiency provided the time step  
235 is small enough. Regarding this last point, in order to improve  
236 the accuracy and efficiency of the simulation, the following  
237 adaptive time step has been applied in the proximity of the  
238 waveguide walls, depending on the electron position:

$$239 \quad \Delta t = \frac{\Delta t_0}{1 + \xi \left( \frac{x - a/2}{a/2} \right)^2 + \xi \left( \frac{y - d/2}{d/2} \right)^2} \quad (15)$$

240 where  $\Delta t_0$  is the initial reference time step,  $\xi$  is a constant  
241 value (in this case, a value of 4.0 has been chosen), and  
242  $x$  and  $y$  are the coordinates of the electron position.

243 As mentioned above, the computed electrons trajectories  
244 may lead to an eventual impact with a surface. Each collision  
245 can result in the emission or absorption of secondary electrons.  
246 A relevant growth in the electron density can develop if the  
247 electrons hit the walls with the appropriate energy and at  
248 suitable instants. The number of electrons emitted or absorbed  
249 after each impact is determined by the value of the Secondary  
250 Electron Yield (SEY) parameter  $\delta$  ( $\delta > 1$  if secondary  
251 electrons are emitted, and  $\delta < 1$  if they are absorbed). The  
252 SEY is modeled by a modification of Vaughan's model [24]  
253 that includes the effect of reflected electrons for low impact  
254 energies of primary electrons, which has to be accounted for to  
255 obtain accurate results [25], [26] in agreement with experimen-  
256 tal data obtained in [27], [28]. The SEY properties for surface  
257 materials can be defined by the following parameters: the  
258 primary electron impact kinetic energies which yield  $\delta = 1$ ,  
259  $W_1$ , and  $W_2$ ; the impact energy  $W_{\max}$  necessary for a primary  
260 electron to yield  $\delta = \delta_{\max}$ , which is the maximum value of the  
261 SEY function; and the value of the primary electron impact  
262 energy  $W_0$  ( $\delta = 0$ ) that limits the region of elastic collisions.

263 When a multipactor discharge evolves in the partially  
264 dielectric-loaded waveguide under study, the dc field distri-  
265 bution has to be updated after each electron impacts on the

TABLE I  
SECONDARY ELECTRON EMISSION YIELD PROPERTIES  
OF DIFFERENT MATERIALS [31], [32]

Material	$W_{\max}$ (eV)	$W_1$ (eV)	$W_2$ (eV)	$W_0$ (eV)	$\delta_{\max}$
Niobium	200.0	33	1500	–	1.6
Silver	165.0	30	5000	15.99	2.22
Teflon	271.7	27	5000	6.81	2.47

dielectric surface. However, tracking the evolution of all the electrons involved in the multipactor discharge would suppose a big computational cost. Thus, we have made use of an EEM, but considering both the spread in secondary emission energy and the angle of the secondary electrons after each impact on the waveguide walls. This assumption has proved to account properly for the charging of the dielectric material, given that the discharging time for dielectrics is much higher than the typical time for a multipactor discharge. Thus, in the EEM assumed in this paper, after the effective electron impacts at time  $t$  with any surface,  $N_i(t)$  is modified according to the  $\delta$  value provided by the SEY function as follows:

$$N_i(t + \Delta t) = \delta N_i(t) \quad (16)$$

where  $N_i(t)$  represents the population of the ee inside the waveguide at the instant  $t$ , and  $\Delta t$  is the time step used in the simulations.

The secondary electron departure kinetic energy  $E_s$  after each electron impact is assumed to fit the following probability density function [29]:

$$\frac{dp(E_s)}{dE_s} = C \exp\left[-\frac{\ln^2(E_s/E_m)}{2\tau^2}\right] \quad (17)$$

where  $C$  is a normalization constant, the parameter  $\tau$  (typical values 0.7–0.8) determines the width of the distribution and  $E_m$  (typical values 3–4 eV) is the energy of the maximum of the spectrum. Finally, the secondary electrons after inelastic impacts are emitted following a cosine distribution of the polar angle.

### III. NUMERICAL RESULTS AND DISCUSSION

An in-house simulation computer-aided design (CAD) tool based on the Monte Carlo method described in Section II has been developed to analyze the multipactor effect in partially dielectric-loaded rectangular waveguides. The first problem analyzed consists of an empty rectangular waveguide previously studied in [14], whose multipactor prediction results have been used for validation purposes. The rectangular waveguide has dimensions  $a = 43.2$  cm and  $b = 10.2$  cm, and is excited by a time-harmonic signal at  $f = 500$  MHz. The material of the waveguide walls is niobium, whose SEY properties are given in Table I and can be expressed with the simple model proposed in [30]. In the algorithm of the simulator used in [14], for each RF power considered in the waveguide, the initial electron is launched at  $x = a/2$ , and the simulation is run 42 times, corresponding to 42 equidistant phases of the RF field. The mean value of the final population of electrons after 20 impacts of the ee against the walls is calculated using all the 42 simulations. Also, the secondary

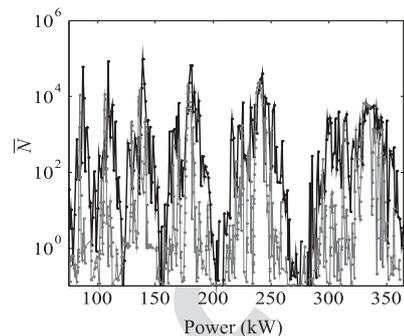


Fig. 2. Comparison with [14] of the mean value of  $N$  over all launch phases in a rectangular waveguide ( $a = 43.1$  cm and  $b = 10.2$  cm) driven at  $f = 500$  MHz with a maximum of 20 impacts from a single initial launch location on the midline of the empty rectangular waveguide.

electrons generated after every collision are launched with an energy of 2 eV normal to the impacting surface. The maximum simulation lifetime of each ee is  $t_{\max} = 1000$  RF cycles, and the simulation is stopped if the impact energy is lower than 0.1 eV or if the accumulated population of electrons is under  $10^{-3}$ . To model the same simulation conditions, our CAD tool has been adapted accordingly. In Fig. 2, the results of the mean population of electrons,  $\bar{N}$ , computed with our code (black lines) are compared with the curves presented in [14] (gray lines). In this figure, we can see some high-risk multipactor power regions. Both curves show a good agreement in the shape and location of these multipactor windows.

Once the model has been validated for an empty waveguide, next we analyze the multipactor effect in a partially dielectric-loaded rectangular waveguide. The selected waveguide configuration for the multipactor analysis is a nonstandard silver-plated rectangular waveguide of width  $a = 19.05$  mm and height  $b = 0.4$  mm, in which a thin dielectric layer has been placed over the bottom surface of the waveguide. A realistic dielectric material has been chosen as teflon (DuPont Teflon fluorinated ethylene propylene Fluoroplastic Film Type), which is a dielectric film commonly used in space applications, of thickness  $h = 0.025$  mm and  $\epsilon_r = 2.1$ ; thus  $d = b - h = 0.375$  mm. Standard values for the SEY parameters of silver [31] are given in Table I, and SEY parameters of teflon have been measured at the ESA-VSC High Power Space Materials Laboratory (Valencia, Spain) [32]. First, a study of the susceptibility chart of this waveguide has been performed. Since it is a partially dielectric-loaded rectangular waveguide, the factor  $f \times d$  is plotted in the horizontal axis of the susceptibility chart. In the vertical axis, it is plotted an effective voltage,  $V_{\text{eff}}$ , which has been calculated numerically as the line integral of the  $E_y$  component of the electric field (evaluated at the center of the waveguide  $x = a/2$ ) from  $y_1 = 0$  to  $y_2 = d$ . To obtain this susceptibility chart for each  $V_{\text{eff}}$  and  $f \times d$  pair, the simulation is run 72 times, corresponding to 72 equidistant initial phases of the RF field separated  $5^\circ$ . In each run, an initial single ee is launched at  $x = a/2$  and  $z = 0$  and at a random position  $y_0$  in the  $y$ -axis between  $y = 0$  and  $y = d$ . The initial electron is launched with a departure kinetic energy given by the probability density function shown in (17) and following

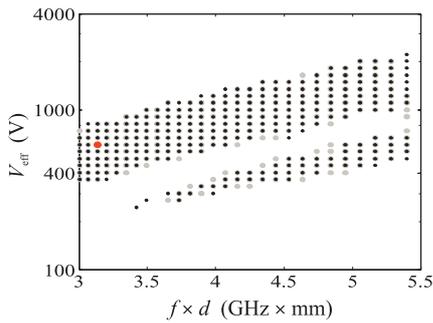


Fig. 3. Comparison of the susceptibility chart of a rectangular waveguide partially filled with teflon (black points) with that of its equivalent empty waveguide (gray points). Red: operating point corresponding to  $f \times d = 3.13 \text{ GHz} \cdot \text{mm}$  and  $V_{\text{eff}} = 608 \text{ V}$ .

a cosine distribution of the polar angle. Each simulation was stopped after 100 RF cycles. In the empty waveguide, the arithmetic mean of the final population of electrons after 100 RF cycles is calculated using all the 72 simulations. If this mean value is greater than 1, then the multipactor discharge is assumed to have occurred. However, in a partially dielectric-loaded waveguide, it has been shown in previous works [8]–[10] that the emission or absorption of electrons by the dielectric surface gives rise to an increasing dc field in the waveguide, which eventually turns off the discharge. Thus, in this case, a minimum mean value of the magnitude of  $E_{\text{dc}}$  field in the waveguide after 100 RF cycles is used as the criterion to assume that a multipactor discharge has occurred at a given operating point.

Fig. 3 shows the computed susceptibility chart of the rectangular waveguide partially filled with teflon (black points). The lowest  $f \times d$  value is above the cutoff frequency of the fundamental mode in this waveguide. In this figure, the susceptibility chart of the equivalent empty waveguide with the same vertical air gap is also represented with gray points for comparison. It can be checked that both the empty and the partially dielectric-loaded waveguide with the same vertical air gap show similar multipactor susceptibility charts, given that the SEY properties of silver and teflon are similar. This susceptibility chart is not generally applicable to any rectangular waveguide with an air gap  $d$ , given that the electromagnetic field distribution depends on the geometry and dimensions of the dielectric layer with respect to the waveguide dimensions, and also on its relative permittivity.

From the results shown earlier, and with the purpose of having a better understanding of the dynamics of the electron inside the partially dielectric-loaded waveguide, a point within the multipactor region has been chosen (highlighted in red in Fig. 3), corresponding to  $V_{\text{eff}} = 608 \text{ V}$  and  $f \times d = 3.13 \text{ GHz} \cdot \text{mm}$ . In this case, the evolution of the multipactor discharge in the partially dielectric-loaded waveguide under study has been analyzed as a function of the time normalized to the RF period. For this simulation, the electron is launched with an initial phase of the RF field  $\varphi_0 = 0^\circ$ . Simulations assuming different initial phases have been performed, and similar results were obtained. The obtained simulation is shown in Fig. 4, where it is plotted the  $y$ -coordinate followed by the ee within the waveguide as a function of the normalized

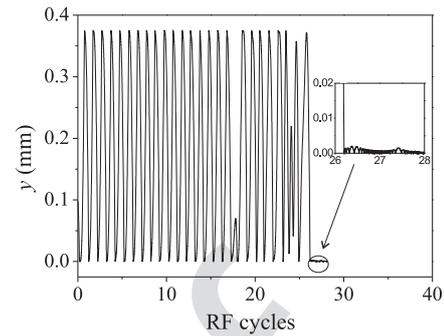


Fig. 4. Trajectory ( $y$ -coordinate) of the ee in the air gap of the rectangular waveguide partially filled with teflon as a function of the RF cycle.

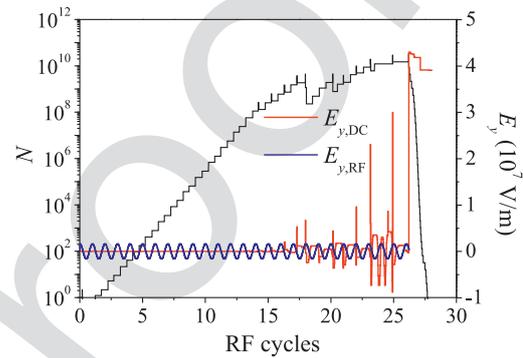


Fig. 5. Black line: time evolution of the total number of electrons  $N$ . Blue line:  $E_{y,\text{RF}}$ . Red line:  $E_{y,\text{dc}}$  at the electron position.

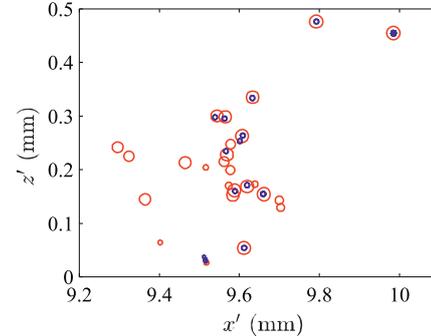


Fig. 6. Distribution of normalized charges  $\bar{Q}_i = Q_i/e$  appearing on the dielectric surface.

time. In the selected multipactor regime, which is inside the multipactor region, the electron initially collides with the top metallic and bottom dielectric surface consecutively in what seems to be a first-order multipactor process during the first 17 RF cycles, remaining in the vicinity of  $x = a/2$  and  $z = 0$ —given that the electron has nearly no acceleration in such directions. As shown in Fig. 5, in the first cycles, the total number of electrons  $N$  (black solid line) follows an exponential growth. This progressive growing of  $N$  makes that the number of charges appearing on the dielectric surface increases, the number which is proportional to the emitted or absorbed electrons in each impact, as seen in Fig. 6 (positive charges are represented with red circles, while negative charges are represented with blue circles; the circles' size is proportional to the charge magnitude in log scale). Such charges on the dielectric interface give rise to the

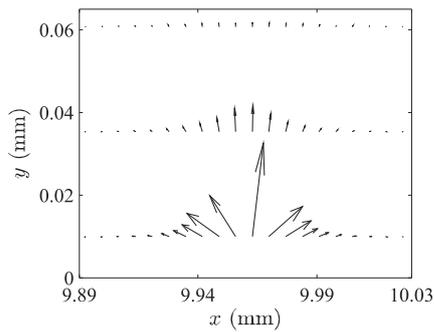


Fig. 7. Transverse distribution of the dc electric field in the proximity of the main charge point in the waveguide air region at RF cycle 26.2, at  $z = 0.45$  mm.

412 appearance of an electrostatic field in the empty gap during  
 413 the time between impacts. Once the population of electrons  
 414 reaches a significant number ( $N \approx 10^9$  in the conditions under  
 415 study), the  $y$ -component of the dc field,  $E_{y,dc}$  [which has been  
 416 plotted in Fig. 5 with red line at the positions  $(x, y, z)$  where  
 417 the effective electron is located in the displayed instants in  
 418 this figure] becomes comparable to  $E_{y,RF}$ , and the effective  
 419 electron is unable to keep up with its previous multipactor  
 420 synchronization. From this moment on, the dc field makes that,  
 421 in some impacts, the electrons collide with the top metallic  
 422 or bottom dielectric surface much sooner or later than the  
 423 instants when the RF electric field changes its sign, which  
 424 implies low impact energy collisions so that electrons are  
 425 absorbed in such impacts. In collisions at the dielectric surface,  
 426 the absorption or emission of electrons yield the appearance  
 427 of growing charges on the dielectric layer, contributing to a  
 428 higher dc field acting on the waveguide. The distribution of  
 429 this high dc field in the proximity of the main charge point  
 430 in the waveguide air region is shown in Fig. 7 at RF cycle  
 431 26.2 in the plane  $z = 0.45$  mm (corresponding to the  $z$   
 432 position of the electron at this instant). The action of this field  
 433 may result in the appearance of a single-surface multipactor  
 434 regime in the dielectric surface [see the  $y$  position of the  
 435 electron in Fig. 4 (inset) from RF cycle 26.2], with successive  
 436 low impact energy collisions, which eventually leads to the  
 437 turning off of the discharge itself (as can be appreciated in  
 438 Fig. 5 from RF cycle 26.2 on). From this instant, the dc field  
 439 distribution in the waveguide remains nearly constant, given  
 440 that  $N$  drops very quickly. The final value of the  $y$ -component  
 441 of the dc field accounts for the balance between the emitted  
 442 and absorbed electrons by the dielectric surface in the whole  
 443 process. Then, although the final population of electrons after  
 444 RF cycle 100 is 0, the remaining high dc field in the waveguide  
 445 indicates that a multipactor discharge has taken place in the  
 446 waveguide in this simulation. It is worth mentioning that the  
 447 observed turning OFF of the discharge observed in the last  
 448 stages of the multipactor evolution in this waveguide has been  
 449 speeded up due to the use of the EEM, although this does not  
 450 change qualitatively the dynamics of the discharge under these  
 451 conditions.

#### IV. CONCLUSION

452  
 453 A study of the multipactor effect in a partially dielectric-  
 454 loaded rectangular waveguide has been carried out. In this

paper, we have considered the RF electromagnetic fields  
 (obtained with a very efficient vectorial modal method) as  
 well as the dc field caused by the appearance of a charge  
 distribution in the dielectric layer. The solution of the elec-  
 trostatic problem has required the use of different numeri-  
 cal integration techniques and interpolation methods. The  
 electron trajectory has been numerically solved by using a  
 Velocity Verlet algorithm, providing sufficient accuracy and  
 good efficiency. As a first example, the multipactor prediction  
 results of an empty rectangular waveguide have been obtained  
 for validation purposes. Second, the susceptibility chart of  
 a partially dielectric-loaded rectangular waveguide has been  
 computed, and the time evolution of a discharge in this  
 waveguide has been studied and discussed. The performed  
 simulations reveal that multipactor discharges in this type of  
 dielectric-loaded waveguides turn OFF by themselves due to  
 the electrostatic field associated with the dielectric surface  
 charges that evolve with the multipactor process.

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# Analysis of Multipactor Effect in a Partially Dielectric-Loaded Rectangular Waveguide

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and Benito Gimeno<sup>3</sup>, Member, IEEE

**Abstract**—This paper presents a study of the multipactor effect in a partially dielectric-loaded rectangular waveguide. To obtain the simulations presented in this paper, a detailed analysis of the dynamics of the electron inside this waveguide has been performed, taking into account the radio frequency electromagnetic fields propagating in the waveguide and the dc electric field that appears because of the charging of the dielectric layer. This electrostatic field is obtained by computing the electric potential produced by an arbitrary charge distribution on the dielectric layer in a dielectric-loaded waveguide. The electron trajectory is then found by numerically solving the equations of motion. The results obtained show that multipactor discharges do turn off by themselves under certain circumstances when they occur in such dielectric-loaded waveguide.

**Index Terms**—Multipactor, secondary emission, waveguide.

## I. INTRODUCTION

MULTIPACTOR is a high-power resonant electron discharge frequently observed in the microwave and millimeter-wave subsystems operating under vacuum conditions [1] present in a wide range of different scenarios, such as passive components of satellite communication payloads, traveling-wave, tubes or particle accelerators. In an ultrahigh vacuum environment, the free electrons inside a microwave device are accelerated by the radio frequency (RF) electromagnetic fields, impacting against its metallic walls. If the electron impact energy is high enough, one or more secondary electrons might be released from the surface. When some resonance conditions are satisfied, the secondary electrons get synchronized with the RF fields, and the electron population inside the device grows exponentially leading to a multipactor discharge. This multipactor discharge has some negative effects that degrade the device performance: increase

of signal noise and reflected power, heating of the device walls, outgassing, detuning of resonant cavities, and even the partial or total destruction of the component.

Multipactor research lines are aimed to study and characterize the phenomenon to predict the conditions for its appearance [2], [3]. Some RF devices, such as filters, multiplexers, and RF satellite payloads, include dielectric materials commonly employed as resonators and supporting elements. In [4], it is presented a review of multipactor discharge on metals and dielectric windows that takes into account the surface materials, and the effects of space charge and cavity loading. The multipactor effect including the presence of dielectric materials in single-surface multipactor regime has been widely investigated in the context of particle accelerators; for instance, in ceramic RF windows [5], [6] and in alumina-based dielectric-loaded accelerating structures [7]. In contrast, very few contributions can be found about multipactor breakdown on dielectrics in the scenario of RF systems for space applications [8]–[10], and mostly under the parallel-plate waveguide approximation. In [11] and [12], the effective electron model (EEM) has been successfully used for simulations of multipaction experiments in coaxial transmission lines considering the presence of external magnetic static fields, demonstrating the validity of this method in complex scenarios. The multipactor inside an empty rectangular waveguide has also been studied in [13] and [14], where the conventional resonance theory gives correct predictions for the multipactor threshold if the height of the waveguide is very small and first-order resonance multipactor dominates. When the waveguide height exceeds a certain critical value, which depends on the waveguide width, an accurate prediction of the multipactor threshold requires considering the RF fields inside the waveguide without approximations. Therefore, there is a need to accurately predict the electron discharge on devices involving partially dielectric-loaded rectangular waveguides, which are of more practical interest for satellite technology. The main aim of this investigation is to extend the results of previous works [8]–[10], where an EEM was successfully applied to study the multipactor in a parallel-plate dielectric-loaded waveguide, to the analysis of multipactor effect in a partially dielectric-loaded rectangular waveguide.

In Section II, the theoretical model employed for the simulations is discussed. In Section III, the multipactor prediction results of an empty rectangular waveguide are analyzed and compared with results from the technical literature for validation purposes. Then, the susceptibility chart of a partially

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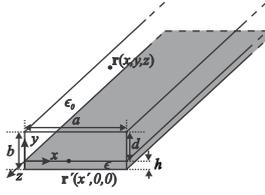


Fig. 1. Geometry and dimensions of the problem under investigation.

monomode regime, where only the fundamental mode,  $\text{TM}_{10}^y$ , propagates in the waveguide. The instantaneous field vectors interacting with the effective electron are given by

$$\mathbf{E}_{\text{RF}}(x, y, z, t) = E_0 \Re\{\mathbf{e}(x, y) e^{j(\omega t - \beta z + \varphi_0)}\} \quad (1a)$$

$$\mathbf{H}_{\text{RF}}(x, y, z, t) = H_0 \Re\{\mathbf{h}(x, y) e^{j(\omega t - \beta z + \varphi_0)}\} \quad (1b)$$

where  $\varphi_0$  is the initial phase and  $E_0, H_0$  are the constants related to the transmitted power in the waveguide. The modal fields  $\mathbf{e}(x, y)$  and  $\mathbf{h}(x, y)$  and the propagation constant  $\beta$  of the  $\text{TM}_{10}^y$  mode can be found in [18] and [19]. These expressions can be directly extended if higher order modes must be taken into account (i.e., in waveguide discontinuities) by using the mode-matching technique.

The key to understanding the mechanism of a multipactor discharge is to study the behavior of the electrons within the waveguide, which are accelerated by the aforementioned electromagnetic fields  $\mathbf{E}_{\text{RF}}$  and  $\mathbf{H}_{\text{RF}}$ . In this way, sooner or later, these fields will make an electron impact with any surface of the rectangular waveguide, which can result in the emission or absorption of secondary electrons. If the impacts occur on the dielectric surface, unlike the case of impacts on the metallic walls, the secondary electrons emitted by the dielectric give rise to positive charges at the impact positions on the dielectric surface, while the electrons absorbed in the dielectric layer will generate negative charges in it. These charges, which are located on the dielectric surface at positions  $\mathbf{r}' = (x', 0, z')$ , give rise to an electrostatic field  $\mathbf{E}_{\text{dc}}$ , which has to be added to the RF fields to obtain accurately the trajectory of the electrons inside the waveguide. In order to determine the electrostatic field,  $\mathbf{E}_{\text{dc}}(x, y, z) = -\nabla\phi(x, y, z)$ , generated by the charges on the dielectric, the potential  $\phi(x, y, z)$  inside the waveguide has to be first calculated. Using the superposition, the potential in the waveguide due to the set of charges  $Q_i$  on the dielectric surface can be obtained by adding the individual contribution of each charge

$$\phi(x, y, z) = \sum_i G(x - x'_i, y, |z - z'_i|) Q_i(x'_i, 0, z'_i) \quad (2)$$

where  $G(x, y, z)$  is the electrostatic potential due to a unit point charge, that is, Green's function for this problem.

The above-mentioned Green's function,  $G(x, y, z)$ , is the solution to the following Laplace's equation [20], [21]:

$$\nabla \cdot [\epsilon_r(y) \nabla G(x, y, z)] = -\frac{1}{\epsilon_0} \delta(x - x') \delta(y) \delta(z) \quad (3)$$

where  $\epsilon_0$  is the free-space dielectric permittivity and the position of the unit charge is taken at  $(x', 0, 0)$  for convenience. Both the geometric characteristics and the linear nature of the problem under consideration makes that the Dirac delta functions can be expressed as [21]

$$\delta(x - x') = \frac{2}{a} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') \quad (4)$$

$$\delta(z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-jk_z z} dk_z \quad (5)$$

where  $k_{xn} = n\pi/a$  and  $k_z$  is the spectral Fourier variable along the longitudinal direction  $z$ . The above-mentioned expressions

79 dielectric-loaded rectangular waveguide is obtained with the  
80 developed model, and the time evolution of a discharge in  
81 this waveguide is studied and discussed. Finally, Section IV  
82 outlines the main conclusions of this paper.

## 83 II. THEORY

### 84 A. Computation of RF and DC Fields in a Partially 85 Dielectric-Loaded Waveguide

86 Fig. 1 shows the scheme of a partially dielectric-loaded  
87 rectangular waveguide of width  $a$  and height  $b$ , and whose  
88 dielectric material has relative permittivity  $\epsilon_r$ . In the problem  
89 under study, the dielectric slab of thickness  $h$  and width  $a$  is  
90 placed over the bottom waveguide wall, being  $d$  the empty  
91 waveguide height where the effective electron travels (see  
92 Fig. 1). The RF electromagnetic field is assumed to propagate  
93 along the positive direction of the  $z$ -axis. For the sake of  
94 simplicity, the waveguide is supposed to be infinite along the  
95  $z$  direction, and a time-harmonic dependence of the type  $e^{j\omega t}$   
96 is implicitly assumed, with  $f = \omega/2\pi$  being the frequency  
97 and  $t$  the time measured in the laboratory reference sys-  
98 tem. To analyze the multipactor evolution in this waveguide,  
99 a multipactor simulation code based on the Monte Carlo  
100 method has been developed. The software code, similar to the  
101 one described in [8] and [9], employs the single EEM [15].  
102 This assumption avoids the consideration of space-charge  
103 effects, what is a strong simplification. The space-charge  
104 effects are often neglected in the analysis of the first stages of  
105 the multipactor discharge [13], [14], but they are doubtless  
106 important at high electron populations when the discharge  
107 is fully developed. Simulation results of some published  
108 works [16], [17] indicate an important role of space-charge in  
109 the evolution of the multipactor process to a saturation stage.  
110 In this paper, however, we are mainly interested in studying  
111 the influence of dielectric charging in the multipactor process.  
112 The inclusion of space-charge effects, although providing a  
113 more realistic description of the global process, would increase  
114 the computational burden very much, as the dc field due  
115 to dielectric charging has to be evaluated in every effective  
116 electron position. In addition, the interpretation of simulation  
117 results would become difficult, as dielectric charging and space  
118 charge can both lead to a repulsion of the freshly emitted  
119 secondary electrons back to the surface.

120 The effective electron at  $\mathbf{r} = (x, y, z)$  can move in the  
121 air region of height  $d$  of the rectangular waveguide. The  
122 electromagnetic fields  $\mathbf{E}_{\text{RF}}$  and  $\mathbf{H}_{\text{RF}}$  acting on the effective  
123 electron correspond to the modes of the partially dielectric-  
124 loaded rectangular waveguide (Fig. 1), which are hybrid modes  
125 of  $\text{TM}^y$  and  $\text{TE}^y$  kinds [18]. We have restricted our study to the

175 come from the fact that the eigenfunctions of the differential  
176 operator are sinusoidal functions along  $x$ -axis and complex  
177 exponential functions along the  $z$ -axis, respectively. This is  
178 equivalent to apply the discrete sine transform along the  $x$ -axis  
179 and the integral transform along the  $z$ -axis, namely,

$$180 \quad G = \frac{1}{\pi a} \int_{-\infty}^{\infty} dk_z e^{-jk_z z} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') \tilde{G} \quad (6)$$

$$181 \quad \tilde{G} = \int_{-\infty}^{\infty} dz e^{jk_z z} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') G \quad (7)$$

182 where  $G = G(x, x', y, z)$  and  $\tilde{G} = \tilde{G}(k_{xn}, k_z; y)$ .

183 According to the above-mentioned considerations, (3) can  
184 be expressed as the following ordinary differential equation  
185 for the spectral Green's function  $\tilde{G}$ :

$$186 \quad \left\{ \frac{d}{dy} \epsilon_r(y) \frac{d}{dy} - k_t^2 \right\} \tilde{G} = -\frac{\delta(y)}{\epsilon_0} \quad (8a)$$

$$187 \quad \tilde{G}(y = -h) = 0 \quad (8b)$$

$$188 \quad \tilde{G}(y = d) = 0 \quad (8c)$$

189 where  $k_t^2 = k_{xn}^2 + k_z^2$ . Solving (8), the following expression  
190 for  $\tilde{G}$  is obtained in the air region  $y \geq 0$ :

$$191 \quad \tilde{G}(k_{xn}, k_z; y) = \frac{\sinh[k_t(d - y)]}{\epsilon_0 k_t [\epsilon_r \coth(k_t h) + \coth(k_t d)] \sinh(k_t d)}. \quad (9)$$

193 Green's function in the spatial domain,  $G$ , is achieved by  
194 replacing (9) into (6) to give

$$195 \quad G(x, x', y, z) \\ 196 \quad = \frac{2}{\epsilon_0 \pi a} \sum_{n=1}^{\infty} \sin(k_{xn}x) \sin(k_{xn}x') \\ 197 \quad \times \int_0^{\infty} \frac{\sinh[k_t(d - y)] \cos(k_z z)}{k_t [\epsilon_r \coth(k_t h) + \coth(k_t d)] \sinh(k_t d)} dk_z. \quad (10)$$

198 In (10), if the point charge is placed at  $z' \neq 0$ ,  $z$  must  
199 be replaced by  $(z - z')$ . Here, it is worth noting that very  
200 efficient numerical summation and integration techniques have  
201 to be employed to compute Green's function with sufficient  
202 accuracy and tolerable CPU times [22].

203 Once Green's function has been calculated, the  $\mathbf{E}_{dc}$  field is  
204 obtained by numerical differentiation of (2) by means of the  
205 central difference technique.

### 206 *B. Multipactor Evolution in the Partially* 207 *Dielectric-Loaded Waveguide*

208 Once the RF and dc fields are known at any instant  $t$ ,  
209 the electron dynamics inside the waveguide can be computed,  
210 which is governed by the Lorentz force and related to its linear  
211 momentum

$$212 \quad \mathbf{F}_L = q(\mathbf{E} + \mathbf{v} \times \mathbf{B}) = \frac{d\mathbf{p}}{dt} \quad (11)$$

213 where  $q = -e$  is the electron charge,  $\mathbf{E}$  and  $\mathbf{B} = \mu_0 \mathbf{H}$   
214 are the total electric and magnetic fields (both RF and dc

215 contributions) interacting with the electron,  $\mu_0$  is the free-  
216 space magnetic permeability, and  $\mathbf{v}$  is the velocity vector of  
217 the electron. The linear relativistic momentum is defined as

$$218 \quad \mathbf{p} = m_0 \gamma \mathbf{v} \quad (12)$$

219 where  $m_0$  is the electron rest mass,  $\gamma = 1/\sqrt{1 - (v/c)^2}$  the  
220 Lorentz factor,  $v$  is the magnitude of the velocity vector, and  
221  $c = 1/\sqrt{\mu_0 \epsilon_0}$  the speed of light in vacuum. Although the  
222 relativistic correction in this equation can be discarded for the  
223 typical power ranges of most space waveguide devices, it must  
224 be considered when high velocities are reached ( $v/c \geq 0.1$ ),  
225 as in high-power multipactor simulations. Expanding (11),  
226 the following differential equation is obtained:

$$227 \quad -\mathbf{E} - \mathbf{v} \times \mathbf{B} = M \gamma \mathbf{a} + \frac{M}{c^2} \gamma^3 (\mathbf{v} \cdot \mathbf{a}) \mathbf{v} \quad (13)$$

228 where  $\mathbf{a}$  is the acceleration vector and  $M = m_0/e$ . The  
229 differential equation to be solved becomes

$$230 \quad \ddot{\mathbf{r}} = \frac{-\dot{\mathbf{r}} \times \mathbf{B} - \mathbf{E} + \dot{\mathbf{r}} \cdot (\dot{\mathbf{r}} \cdot \mathbf{E})/c^2}{M \gamma}. \quad (14)$$

231 The electron trajectory is found by numerically solving  
232 the above-mentioned equations of motion. For that purpose,  
233 a Velocity Verlet algorithm [23] has been used, which assures  
234 sufficient accuracy and good efficiency provided the time step  
235 is small enough. Regarding this last point, in order to improve  
236 the accuracy and efficiency of the simulation, the following  
237 adaptive time step has been applied in the proximity of the  
238 waveguide walls, depending on the electron position:

$$239 \quad \Delta t = \frac{\Delta t_0}{1 + \xi \left( \frac{x - a/2}{a/2} \right)^2 + \xi \left( \frac{y - d/2}{d/2} \right)^2} \quad (15)$$

240 where  $\Delta t_0$  is the initial reference time step,  $\xi$  is a constant  
241 value (in this case, a value of 4.0 has been chosen), and  
242  $x$  and  $y$  are the coordinates of the electron position.

243 As mentioned above, the computed electrons trajectories  
244 may lead to an eventual impact with a surface. Each collision  
245 can result in the emission or absorption of secondary electrons.  
246 A relevant growth in the electron density can develop if the  
247 electrons hit the walls with the appropriate energy and at  
248 suitable instants. The number of electrons emitted or absorbed  
249 after each impact is determined by the value of the Secondary  
250 Electron Yield (SEY) parameter  $\delta$  ( $\delta > 1$  if secondary  
251 electrons are emitted, and  $\delta < 1$  if they are absorbed). The  
252 SEY is modeled by a modification of Vaughan's model [24]  
253 that includes the effect of reflected electrons for low impact  
254 energies of primary electrons, which has to be accounted for to  
255 obtain accurate results [25], [26] in agreement with experimen-  
256 tal data obtained in [27], [28]. The SEY properties for surface  
257 materials can be defined by the following parameters: the  
258 primary electron impact kinetic energies which yield  $\delta = 1$ ,  
259  $W_1$ , and  $W_2$ ; the impact energy  $W_{\max}$  necessary for a primary  
260 electron to yield  $\delta = \delta_{\max}$ , which is the maximum value of the  
261 SEY function; and the value of the primary electron impact  
262 energy  $W_0$  ( $\delta = 0$ ) that limits the region of elastic collisions.

263 When a multipactor discharge evolves in the partially  
264 dielectric-loaded waveguide under study, the dc field distri-  
265 bution has to be updated after each electron impacts on the

TABLE I  
SECONDARY ELECTRON EMISSION YIELD PROPERTIES  
OF DIFFERENT MATERIALS [31], [32]

Material	$W_{\max}$ (eV)	$W_1$ (eV)	$W_2$ (eV)	$W_0$ (eV)	$\delta_{\max}$
Niobium	200.0	33	1500	–	1.6
Silver	165.0	30	5000	15.99	2.22
Teflon	271.7	27	5000	6.81	2.47

dielectric surface. However, tracking the evolution of all the electrons involved in the multipactor discharge would suppose a big computational cost. Thus, we have made use of an EEM, but considering both the spread in secondary emission energy and the angle of the secondary electrons after each impact on the waveguide walls. This assumption has proved to account properly for the charging of the dielectric material, given that the discharging time for dielectrics is much higher than the typical time for a multipactor discharge. Thus, in the EEM assumed in this paper, after the effective electron impacts at time  $t$  with any surface,  $N_i(t)$  is modified according to the  $\delta$  value provided by the SEY function as follows:

$$N_i(t + \Delta t) = \delta N_i(t) \quad (16)$$

where  $N_i(t)$  represents the population of the ee inside the waveguide at the instant  $t$ , and  $\Delta t$  is the time step used in the simulations.

The secondary electron departure kinetic energy  $E_s$  after each electron impact is assumed to fit the following probability density function [29]:

$$\frac{dp(E_s)}{dE_s} = C \exp\left[-\frac{\ln^2(E_s/E_m)}{2\tau^2}\right] \quad (17)$$

where  $C$  is a normalization constant, the parameter  $\tau$  (typical values 0.7–0.8) determines the width of the distribution and  $E_m$  (typical values 3–4 eV) is the energy of the maximum of the spectrum. Finally, the secondary electrons after inelastic impacts are emitted following a cosine distribution of the polar angle.

### III. NUMERICAL RESULTS AND DISCUSSION

An in-house simulation computer-aided design (CAD) tool based on the Monte Carlo method described in Section II has been developed to analyze the multipactor effect in partially dielectric-loaded rectangular waveguides. The first problem analyzed consists of an empty rectangular waveguide previously studied in [14], whose multipactor prediction results have been used for validation purposes. The rectangular waveguide has dimensions  $a = 43.2$  cm and  $b = 10.2$  cm, and is excited by a time-harmonic signal at  $f = 500$  MHz. The material of the waveguide walls is niobium, whose SEY properties are given in Table I and can be expressed with the simple model proposed in [30]. In the algorithm of the simulator used in [14], for each RF power considered in the waveguide, the initial electron is launched at  $x = a/2$ , and the simulation is run 42 times, corresponding to 42 equidistant phases of the RF field. The mean value of the final population of electrons after 20 impacts of the ee against the walls is calculated using all the 42 simulations. Also, the secondary

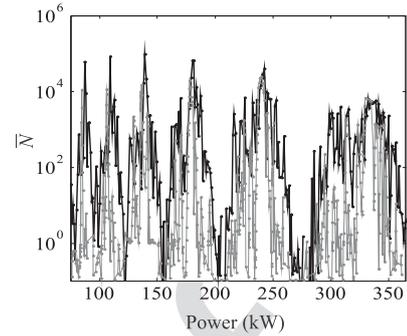


Fig. 2. Comparison with [14] of the mean value of  $N$  over all launch phases in a rectangular waveguide ( $a = 43.1$  cm and  $b = 10.2$  cm) driven at  $f = 500$  MHz with a maximum of 20 impacts from a single initial launch location on the midline of the empty rectangular waveguide.

electrons generated after every collision are launched with an energy of 2 eV normal to the impacting surface. The maximum simulation lifetime of each ee is  $t_{\max} = 1000$  RF cycles, and the simulation is stopped if the impact energy is lower than 0.1 eV or if the accumulated population of electrons is under  $10^{-3}$ . To model the same simulation conditions, our CAD tool has been adapted accordingly. In Fig. 2, the results of the mean population of electrons,  $\bar{N}$ , computed with our code (black lines) are compared with the curves presented in [14] (gray lines). In this figure, we can see some high-risk multipactor power regions. Both curves show a good agreement in the shape and location of these multipactor windows.

Once the model has been validated for an empty waveguide, next we analyze the multipactor effect in a partially dielectric-loaded rectangular waveguide. The selected waveguide configuration for the multipactor analysis is a nonstandard silver-plated rectangular waveguide of width  $a = 19.05$  mm and height  $b = 0.4$  mm, in which a thin dielectric layer has been placed over the bottom surface of the waveguide. A realistic dielectric material has been chosen as teflon (DuPont Teflon fluorinated ethylene propylene Fluoroplastic Film Type), which is a dielectric film commonly used in space applications, of thickness  $h = 0.025$  mm and  $\epsilon_r = 2.1$ ; thus  $d = b - h = 0.375$  mm. Standard values for the SEY parameters of silver [31] are given in Table I, and SEY parameters of teflon have been measured at the ESA-VSC High Power Space Materials Laboratory (Valencia, Spain) [32]. First, a study of the susceptibility chart of this waveguide has been performed. Since it is a partially dielectric-loaded rectangular waveguide, the factor  $f \times d$  is plotted in the horizontal axis of the susceptibility chart. In the vertical axis, it is plotted an effective voltage,  $V_{\text{eff}}$ , which has been calculated numerically as the line integral of the  $E_y$  component of the electric field (evaluated at the center of the waveguide  $x = a/2$ ) from  $y_1 = 0$  to  $y_2 = d$ . To obtain this susceptibility chart for each  $V_{\text{eff}}$  and  $f \times d$  pair, the simulation is run 72 times, corresponding to 72 equidistant initial phases of the RF field separated  $5^\circ$ . In each run, an initial single ee is launched at  $x = a/2$  and  $z = 0$  and at a random position  $y_0$  in the  $y$ -axis between  $y = 0$  and  $y = d$ . The initial electron is launched with a departure kinetic energy given by the probability density function shown in (17) and following

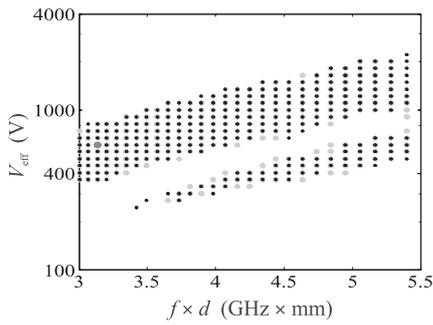


Fig. 3. Comparison of the susceptibility chart of a rectangular waveguide partially filled with teflon (black points) with that of its equivalent empty waveguide (gray points). Red: operating point corresponding to  $f \times d = 3.13 \text{ GHz} \cdot \text{mm}$  and  $V_{\text{eff}} = 608 \text{ V}$ .

a cosine distribution of the polar angle. Each simulation was stopped after 100 RF cycles. In the empty waveguide, the arithmetic mean of the final population of electrons after 100 RF cycles is calculated using all the 72 simulations. If this mean value is greater than 1, then the multipactor discharge is assumed to have occurred. However, in a partially dielectric-loaded waveguide, it has been shown in previous works [8]–[10] that the emission or absorption of electrons by the dielectric surface gives rise to an increasing dc field in the waveguide, which eventually turns off the discharge. Thus, in this case, a minimum mean value of the magnitude of  $E_{\text{dc}}$  field in the waveguide after 100 RF cycles is used as the criterion to assume that a multipactor discharge has occurred at a given operating point.

Fig. 3 shows the computed susceptibility chart of the rectangular waveguide partially filled with teflon (black points). The lowest  $f \times d$  value is above the cutoff frequency of the fundamental mode in this waveguide. In this figure, the susceptibility chart of the equivalent empty waveguide with the same vertical air gap is also represented with gray points for comparison. It can be checked that both the empty and the partially dielectric-loaded waveguide with the same vertical air gap show similar multipactor susceptibility charts, given that the SEY properties of silver and teflon are similar. This susceptibility chart is not generally applicable to any rectangular waveguide with an air gap  $d$ , given that the electromagnetic field distribution depends on the geometry and dimensions of the dielectric layer with respect to the waveguide dimensions, and also on its relative permittivity.

From the results shown earlier, and with the purpose of having a better understanding of the dynamics of the electron inside the partially dielectric-loaded waveguide, a point within the multipactor region has been chosen (highlighted in red in Fig. 3), corresponding to  $V_{\text{eff}} = 608 \text{ V}$  and  $f \times d = 3.13 \text{ GHz} \cdot \text{mm}$ . In this case, the evolution of the multipactor discharge in the partially dielectric-loaded waveguide under study has been analyzed as a function of the time normalized to the RF period. For this simulation, the electron is launched with an initial phase of the RF field  $\varphi_0 = 0^\circ$ . Simulations assuming different initial phases have been performed, and similar results were obtained. The obtained simulation is shown in Fig. 4, where it is plotted the  $y$ -coordinate followed by the ee within the waveguide as a function of the normalized

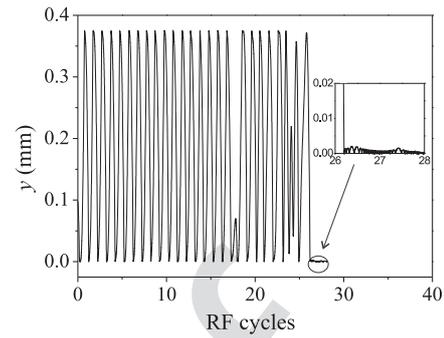


Fig. 4. Trajectory ( $y$ -coordinate) of the ee in the air gap of the rectangular waveguide partially filled with teflon as a function of the RF cycle.

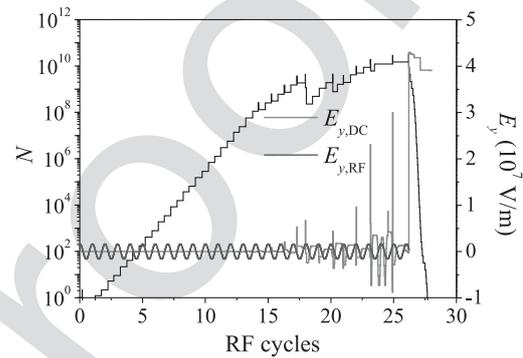


Fig. 5. Black line: time evolution of the total number of electrons  $N$ . Blue line:  $E_{y,\text{RF}}$ . Red line:  $E_{y,\text{dc}}$  at the electron position.

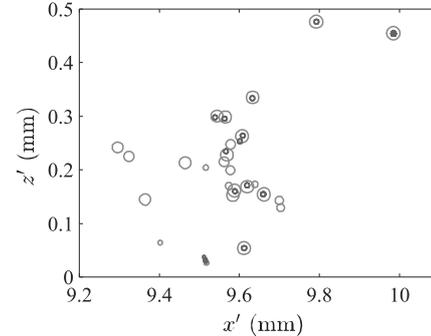


Fig. 6. Distribution of normalized charges  $\bar{Q}_i = Q_i/e$  appearing on the dielectric surface.

time. In the selected multipactor regime, which is inside the multipactor region, the electron initially collides with the top metallic and bottom dielectric surface consecutively in what seems to be a first-order multipactor process during the first 17 RF cycles, remaining in the vicinity of  $x = a/2$  and  $z = 0$ —given that the electron has nearly no acceleration in such directions. As shown in Fig. 5, in the first cycles, the total number of electrons  $N$  (black solid line) follows an exponential growth. This progressive growing of  $N$  makes that the number of charges appearing on the dielectric surface increases, the number which is proportional to the emitted or absorbed electrons in each impact, as seen in Fig. 6 (positive charges are represented with red circles, while negative charges are represented with blue circles; the circles' size is proportional to the charge magnitude in log scale). Such charges on the dielectric interface give rise to the

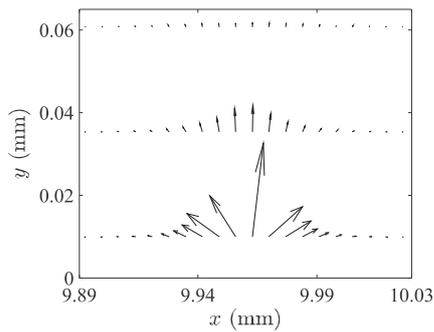


Fig. 7. Transverse distribution of the dc electric field in the proximity of the main charge point in the waveguide air region at RF cycle 26.2, at  $z = 0.45$  mm.

412 appearance of an electrostatic field in the empty gap during  
 413 the time between impacts. Once the population of electrons  
 414 reaches a significant number ( $N \approx 10^9$  in the conditions under  
 415 study), the  $y$ -component of the dc field,  $E_{y,dc}$  [which has been  
 416 plotted in Fig. 5 with red line at the positions  $(x, y, z)$  where  
 417 the effective electron is located in the displayed instants in  
 418 this figure] becomes comparable to  $E_{y,RF}$ , and the effective  
 419 electron is unable to keep up with its previous multipactor  
 420 synchronization. From this moment on, the dc field makes that,  
 421 in some impacts, the electrons collide with the top metallic  
 422 or bottom dielectric surface much sooner or later than the  
 423 instants when the RF electric field changes its sign, which  
 424 implies low impact energy collisions so that electrons are  
 425 absorbed in such impacts. In collisions at the dielectric surface,  
 426 the absorption or emission of electrons yield the appearance  
 427 of growing charges on the dielectric layer, contributing to a  
 428 higher dc field acting on the waveguide. The distribution of  
 429 this high dc field in the proximity of the main charge point  
 430 in the waveguide air region is shown in Fig. 7 at RF cycle  
 431 26.2 in the plane  $z = 0.45$  mm (corresponding to the  $z$   
 432 position of the electron at this instant). The action of this field  
 433 may result in the appearance of a single-surface multipactor  
 434 regime in the dielectric surface [see the  $y$  position of the  
 435 electron in Fig. 4 (inset) from RF cycle 26.2], with successive  
 436 low impact energy collisions, which eventually leads to the  
 437 turning off of the discharge itself (as can be appreciated in  
 438 Fig. 5 from RF cycle 26.2 on). From this instant, the dc field  
 439 distribution in the waveguide remains nearly constant, given  
 440 that  $N$  drops very quickly. The final value of the  $y$ -component  
 441 of the dc field accounts for the balance between the emitted  
 442 and absorbed electrons by the dielectric surface in the whole  
 443 process. Then, although the final population of electrons after  
 444 RF cycle 100 is 0, the remaining high dc field in the waveguide  
 445 indicates that a multipactor discharge has taken place in the  
 446 waveguide in this simulation. It is worth mentioning that the  
 447 observed turning OFF of the discharge observed in the last  
 448 stages of the multipactor evolution in this waveguide has been  
 449 speeded up due to the use of the EEM, although this does not  
 450 change qualitatively the dynamics of the discharge under these  
 451 conditions.

#### IV. CONCLUSION

452 A study of the multipactor effect in a partially dielectric-  
 453 loaded rectangular waveguide has been carried out. In this  
 454

paper, we have considered the RF electromagnetic fields  
 (obtained with a very efficient vectorial modal method) as  
 well as the dc field caused by the appearance of a charge  
 distribution in the dielectric layer. The solution of the elec-  
 trostatic problem has required the use of different numeri-  
 cal integration techniques and interpolation methods. The  
 electron trajectory has been numerically solved by using a  
 Velocity Verlet algorithm, providing sufficient accuracy and  
 good efficiency. As a first example, the multipactor prediction  
 results of an empty rectangular waveguide have been obtained  
 for validation purposes. Second, the susceptibility chart of  
 a partially dielectric-loaded rectangular waveguide has been  
 computed, and the time evolution of a discharge in this  
 waveguide has been studied and discussed. The performed  
 simulations reveal that multipactor discharges in this type of  
 dielectric-loaded waveguides turn OFF by themselves due to  
 the electrostatic field associated with the dielectric surface  
 charges that evolve with the multipactor process.

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